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Algebra • Division Patterns with Decimals

To divide a number by 10, 100, or 1,000, use the number of zeros in the divisor to determine how the position of the decimal point changes in the quotient.

	Number of zeros:	Move decimal point:
$147 \div 1 = \underline{147}$	0	0 places to the left
$147 \div 10 = \underline{14.7}$	1	1 place to the left
$147 \div 100 = \underline{1.47}$	2	2 places to the left
$147 \div 1,000 = \underline{0.147}$	3	3 places to the left

To divide a number by a power of 10, you can use the exponent to determine how the position of the decimal point changes in the quotient.

	Exponent	Move decimal point:
$97.2 \div 10^0 = \underline{97.2}$	0	0 places to the left
$97.2 \div 10^1 = \underline{9.72}$	1	1 place to the left
$97.2 \div 10^2 = \underline{0.972}$	2	2 places to the left

Complete the pattern.

- | | | |
|---|---|---|
| 1. $358 \div 10^0 = \underline{\hspace{2cm}}$ | 2. $102 \div 10^0 = \underline{\hspace{2cm}}$ | 3. $99.5 \div 1 = \underline{\hspace{2cm}}$ |
| $358 \div 10^1 = \underline{\hspace{2cm}}$ | $102 \div 10^1 = \underline{\hspace{2cm}}$ | $99.5 \div 10 = \underline{\hspace{2cm}}$ |
| $358 \div 10^2 = \underline{\hspace{2cm}}$ | $102 \div 10^2 = \underline{\hspace{2cm}}$ | $99.5 \div 100 = \underline{\hspace{2cm}}$ |
| $358 \div 10^3 = \underline{\hspace{2cm}}$ | $102 \div 10^3 = \underline{\hspace{2cm}}$ | |

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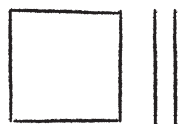
Divide Decimals by Whole Numbers

You can draw a quick picture to help you divide a decimal by a whole number.

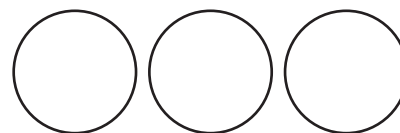
In a decimal model, each large square represents one, or 1. Each bar represents one-tenth, or 0.1.

Divide. $1.2 \div 3$

Step 1 Draw a quick picture to represent the dividend, 1.2.



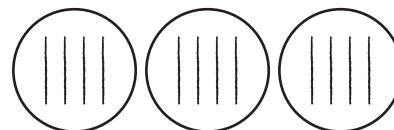
Step 2 Draw 3 circles to represent the divisor, 3.



Step 3 You cannot evenly divide 1 into 3 groups. Regroup 1 as 10 tenths. There are 12 tenths in 1.2.



Step 4 Share the tenths equally among 3 groups.



Each group contains 0 ones and 4 tenths.

So, $1.2 \div 3 = \underline{0.4}$.

Divide. Draw a quick picture.

1. $2.7 \div 9 = \underline{\hspace{2cm}}$

2. $4.8 \div 8 = \underline{\hspace{2cm}}$

3. $2.8 \div 7 = \underline{\hspace{2cm}}$

4. $7.25 \div 5 = \underline{\hspace{2cm}}$

5. $3.78 \div 3 = \underline{\hspace{2cm}}$

6. $8.52 \div 4 = \underline{\hspace{2cm}}$

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Estimate Quotients

You can use multiples and compatible numbers to estimate decimal quotients.

Estimate. $249.7 \div 31$

Step 1 Round the divisor, 31, to the nearest 10.

31 rounded to the nearest 10 is 30.

Step 2 Find the multiples of 30 that the dividend, 249.7, is between.

249.7 is between 240 and 270.

Step 3 Divide each multiple by the rounded divisor, 30.

$240 \div 30 = \underline{8}$ $270 \div 30 = \underline{9}$

So, two possible estimates are 8 and 9.

Use compatible numbers to estimate the quotient.

1. $23.6 \div 7$

_____ \div _____ = _____

2. $469.4 \div 62$

_____ \div _____ = _____

Estimate the quotient.

3. $338.7 \div 49$

4. $75.1 \div 9$

5. $674.8 \div 23$

6. $61.9 \div 7$

7. $96.5 \div 19$

8. $57.2 \div 8$

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Division of Decimals by Whole Numbers

Divide. $19.61 \div 37$

Step 1 Estimate the quotient.

$2,000 \text{ hundredths} \div 40 = \underline{50}$ hundredths, or 0.50.
So, the quotient will have a zero in the ones place.

$$\begin{array}{r} 0 \\ 37 \overline{)19.61} \end{array}$$

Step 2 Divide the tenths.

Use the estimate. Try 5 in the tenths place.

Multiply. $\underline{5} \times 37 = \underline{185}$

Subtract. $196 - \underline{185} = \underline{11}$

Check. $\underline{11} < 37$

$$\begin{array}{r} 0.5 \\ 37 \overline{)19.61} \\ - 185 \\ \hline 11 \end{array}$$

Step 3 Divide the hundredths.

Estimate: $120 \text{ hundredths} \div 40 = 3 \text{ hundredths}$.

Multiply. $\underline{3} \times 37 = \underline{111}$

Subtract. $\underline{111} - \underline{111} = \underline{0}$

Check. $\underline{0} < 37$

Place the decimal point in the quotient.

So, $19.61 \div 37 = \underline{0.53}$.

$$\begin{array}{r} 0.53 \\ 37 \overline{)19.61} \\ - 185 \\ \hline 111 \\ - 111 \\ \hline 0 \end{array}$$

Write the quotient with the decimal point placed correctly.

1. $5.94 \div 3 = 198$ _____

2. $48.3 \div 23 = 21$ _____

Divide.

3. $9 \overline{)61.2}$

4. $17 \overline{)83.3}$

5. $9 \overline{)7.38}$

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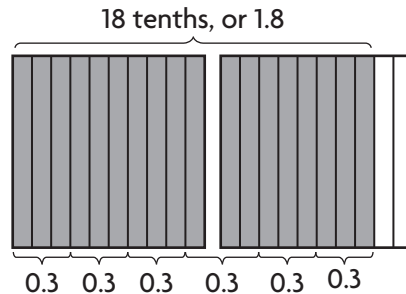
Decimal Division

You can use decimal models to divide tenths.

Divide. $1.8 \div 0.3$.

Step 1 Shade 18 tenths to represent the dividend, 1.8.

Step 2 Divide the 18 tenths into groups of 3 tenths to represent the divisor, 0.3.



Step 3 Count the groups.

There are 6 groups of 0.3 in 1.8. So, $1.8 \div 0.3 = \underline{6}$.

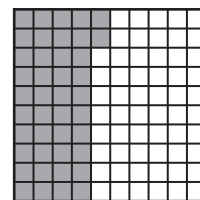
You can use decimal models to divide hundredths.

Divide. $0.42 \div 0.06$

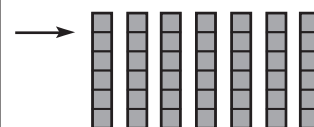
Step 1 Shade 42 squares to represent the dividend, 0.42.

Step 2 Divide the 42 small squares into groups of 6 hundredths to represent the divisor, 0.06.

There are 42 shaded squares, or 0.42.



There are 7 groups of 6 hundredths.

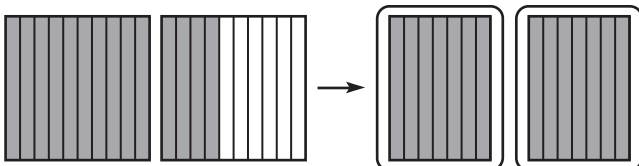


Step 3 Count the groups.

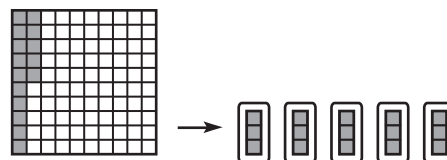
There are 7 groups of 0.06 in 0.42. So, $0.42 \div 0.06 = \underline{7}$.

Use the model to complete the number sentence.

1. $1.4 \div 0.7 = \underline{\hspace{2cm}}$



2. $0.15 \div 0.03 = \underline{\hspace{2cm}}$



Divide. Use decimal models.

3. $2.7 \div 0.3 = \underline{\hspace{2cm}}$ 4. $0.52 \div 0.26 = \underline{\hspace{2cm}}$ 5. $0.96 \div 0.16 = \underline{\hspace{2cm}}$

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Divide Decimals

You can multiply the dividend and the divisor by the same power of 10 to make the divisor a whole number. As long as you multiply both the dividend and the divisor by the same power of 10, the quotient stays the same.

Example 1: Divide. $0.84 \div 0.07$

Multiply the dividend, 0.84, and the divisor, 0.07, by the power of 10 that makes the divisor a whole number.

$$\begin{array}{r} 0.84 \div 0.07 = ? \\ \downarrow \quad \downarrow \\ \times 100 \quad \times 100 \\ \downarrow \quad \downarrow \\ \underline{84} \div \underline{7} = 12 \end{array}$$

Since $84 \div 7 = 12$, you know that $0.84 \div 0.07 = \underline{12}$.

Example 2: Divide. $4.42 \div 3.4$

Multiply both the dividend and the divisor by 10 to make the divisor a whole number.

$$3.4 \overline{)4.42} \xrightarrow{\text{Multiply 3.4 and 4.42 both by 10}} 34 \overline{)44.2}$$

Divide as you would whole numbers. Place the decimal point in the quotient, above the decimal point in the dividend.

$$\begin{array}{r} 1.3 \\ 34 \overline{)44.2} \\ \underline{-34} \\ 102 \\ \underline{-102} \\ 0 \end{array}$$

So, $4.42 \div 3.4 = \underline{1.3}$.

Copy and complete the pattern.

1. $54 \div 6 = \underline{\hspace{2cm}}$

2. $184 \div 23 = \underline{\hspace{2cm}}$

3. $138 \div 2 = \underline{\hspace{2cm}}$

$5.4 \div \underline{\hspace{2cm}} = 9$

$18.4 \div \underline{\hspace{2cm}} = 8$

$13.8 \div \underline{\hspace{2cm}} = 69$

$\underline{\hspace{2cm}} \div 0.06 = 9$

$\underline{\hspace{2cm}} \div 0.23 = 8$

$\underline{\hspace{2cm}} \div 0.02 = 69$

Divide.

4. $1.4 \overline{)9.8}$

5. $0.3 \overline{)0.6}$

6. $3.64 \div 1.3$

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Write Zeros in the Dividend

When there are not enough digits in the dividend to complete the division, you can write zeros to the right of the last digit in a decimal number in the dividend. Writing zeros to the right of the last digit will not change the value of the dividend or the quotient.

Divide. $5.2 \div 8$

Step 1 Divide as you would whole numbers. Place the decimal point in the quotient above the decimal point in the dividend.

$$\begin{array}{r} 0.6 \\ 8 \overline{)5.2} \\ \underline{-48} \\ 4 \end{array}$$

The decimal point in the quotient is directly above the decimal point in the dividend.

Step 2 The difference is less than the divisor. Write a 0 in the dividend to the right of the last digit and continue to divide.

$$\begin{array}{r} 0.65 \\ 8 \overline{)5.20} \\ \underline{-48} \\ 40 \\ \underline{-40} \\ 0 \end{array}$$

The difference, 4, is less than the divisor.

Write a 0 in the dividend to the right of the last digit. Then continue to divide.

So, $5.2 \div 8 = \underline{0.65}$.

Write the quotient with the decimal point placed correctly.

1. $3 \div 0.4 = 75$ 2. $25.2 \div 8 = 315$ 3. $60 \div 25 = 24$ 4. $8.28 \div 0.72 = 115$

Divide.

5. $6 \overline{)43.5}$ 6. $1.4 \overline{)7.7}$ 7. $30 \overline{)72}$ 8. $0.18 \overline{)0.63}$

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Problem Solving • Decimal Operations

Rebecca spent \$32.55 for a photo album and three identical candles. The photo album cost \$17.50 and the sales tax was \$1.55. How much did each candle cost?

Read the Problem		
What do I need to find?	What information do I need to use?	How will I use the information?
I need to find <u>the cost of each candle</u> .	Rebecca spent <u>\$32.55</u> for a photo album and <u>3</u> candles. The photo album cost <u>\$17.50</u> . The sales tax was <u>\$1.55</u> .	I can <u>use a flowchart and work backward from the total amount Rebecca spent to find the cost of each candle.</u>
Solve the Problem		
<ul style="list-style-type: none"> Make a flowchart to show the information. Then work backward to solve. 		
<p style="text-align: center;"> $\begin{array}{ccccccc} \boxed{\text{Cost of 3 candles}} & \xrightarrow{\text{plus}} & \boxed{\text{Cost of photo album}} & \xrightarrow{\text{plus}} & \boxed{\text{Sales tax}} & \xrightarrow{\text{equals}} & \boxed{\text{Total spent}} \\ 3 \times \text{cost of each candle} & + & \\$17.50 & + & \\$1.55 & = & \\$32.55 \end{array}$ </p>		
<p style="text-align: center;"> $\begin{array}{ccccccc} \boxed{\text{Total spent}} & \xrightarrow{\text{minus}} & \boxed{\text{Sales tax}} & \xrightarrow{\text{minus}} & \boxed{\text{Cost of photo album}} & \xrightarrow{\text{equals}} & \boxed{\text{Cost of 3 candles}} \\ \\$32.55 & - & \\$1.55 & - & \\$17.50 & = & \\$13.50 \end{array}$ </p>		
<ul style="list-style-type: none"> Divide the cost of 3 candles by 3 to find the cost of each candle. <u>\$13.50</u> ÷ 3 = <u>\$4.50</u> <p>So, each candle cost \$4.50.</p>		

Use a flowchart to help you solve the problem.

1. Maria spent \$28.69 on one pair of jeans and two T-shirts. The jeans cost \$16.49. Each T-shirt cost the same amount. The sales tax was \$1.62. How much did each T-shirt cost?
2. At the skating rink, Sean and Patrick spent \$17.45 on admission and snacks. They used one coupon for \$2 off the admission. The snacks cost \$5.95. What is the regular admission cost for one?