

# **Add and Subtract Fractions**

## Show What You Know

Check your understanding of important skills

Name .

**Fractions Equal to 1** Write the fraction that names the whole.





Parts of a Whole Write a fraction that names the shaded part.







Read and Write Fractions Write a fraction for the shaded part. Write a fraction for the unshaded part.

6.				7.	
		_	shaded:	-	shaded:
			unshaded:		unshaded:



The electricity that powers our appliances is converted from many sources of energy. About  $\frac{5}{10}$  is made from coal, about  $\frac{2}{10}$  from natural gas, and about  $\frac{2}{10}$  from nuclear power. Be a Math Detective. About how much of our electricity comes from sources other than coal, natural gas, or nuclear power?



## **Vocabulary Builder**

Complete the bubble map using the words with a  $\checkmark$ .

Visualize It ••••••





## Understand Vocabulary •••••

Write the word or phrase that matches the description.

- **1.** When the numerator and denominator have only 1 as a common factor
- 2. A number that names a part of a whole or part of a group

3. An amount given as a whole number and a fraction

4. The number in a fraction that tells how many equal parts

are in the whole or in the group \_\_\_\_\_

A fraction that has a numerator of one \_\_\_\_\_\_

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#### Name \_

## Add and Subtract Parts of a Whole

Essential Question When can you add or subtract parts of a whole?

## Investigate

**Materials** fraction circles color pencils

Ms. Clark has the following pie pieces left over from a bake sale.





She will combine the pieces so they are on the same dish. How much pie will be on the dish?

**A.** Model the problem using fraction circles. Draw a picture of your model. Then write the sum.



So, \_\_\_\_\_ of a pie is on the dish.

**B.** Suppose Ms. Clark eats 2 pieces of the pie. How much pie will be left on the dish? Model the problem using fraction circles. Draw a picture of your model. Then write the difference.



## **Draw Conclusions** .

**1.** Kevin says that when you combine 3 pieces of pie and 1 piece of pie, you have 4 pieces of pie. **Explain** how Kevin's statement is related to the equation  $\frac{3}{6} + \frac{1}{6} = \frac{4}{6}$ .

- **2.** Isabel wrote the equation  $\frac{1}{2} + \frac{1}{6} = \frac{4}{6}$  and Jonah wrote  $\frac{3}{6} + \frac{1}{6} = \frac{4}{6}$  to represent combining the pie pieces. Explain why both equations are correct.
- **3.** There is  $\frac{4}{6}$  of a pie on a plate, what part of the pie is missing from the plate? Write an equation to justify your answer.

## **Make Connections**

You can only join or separate parts that refer to the same whole.

Suppose Randy has  $\frac{1}{4}$  of a round cake and  $\frac{1}{4}$  of a square cake.





	MATHEMATICAL PRACTICES
Math Talk	Give an example of a situation
where th	e equation $\frac{1}{4} + \frac{1}{4} = \frac{2}{4}$ makes
sense. Ex	plain your reasoning.

- a. Are the wholes the same? Explain.
- **b.** Does the sum  $\frac{1}{4} + \frac{1}{4} = \frac{2}{4}$  make sense in this situation? Explain.



Use the model to solve the equation.





- 7. Sean has  $\frac{1}{5}$  of a cupcake and  $\frac{1}{5}$  of a large cake.
  - a. Are the wholes the same? Explain.
  - **b.** Does the sum  $\frac{1}{5} + \frac{1}{5} = \frac{2}{5}$  make sense in this situation? Explain.

## Problem Solving REAL WORLD

#### **Sense or Nonsense?**

8. Samantha and Kim used different models to help find  $\frac{1}{3} + \frac{1}{6}$ . Whose model makes sense? Whose model is nonsense? Explain your reasoning below each model.

Samantha's Model

**9.** Draw a model you could use to add  $\frac{1}{4} + \frac{1}{2}$ .

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## Write Fractions as Sums

**Essential Question** How can you write a fraction as a sum of fractions with the same denominators?



 What if Emilio ate 3 pieces of the sandwich instead of 1 piece? How many snack plates would he need? What part of the sandwich would be on each plate? Explain. Lesson 7.2

## **Example 2** Write a fraction as a sum.

Kevin and Olivia are going to share a whole pizza. The pizza is cut into 6 equal slices. They will put the slices on two separate dishes. What part of the whole pizza could be on each dish?

Shade the models to show three different ways Kevin and Olivia could share the pizza. Write an equation for each model.

#### **Think:** $\frac{6}{6} = 1$ whole pizza.



2. What if 3 friends share the pizza and they put the pizza slices on three separate dishes? What part of the pizza could be on each dish? Write equations to support your answer.

Name .

# Share and Show

**1.** Write  $\frac{3}{4}$  as a sum of unit fractions.



#### Write the fraction as a sum of unit fractions.



6		
9. a.	Holly's garden is divided into 5 equal section the garden into 3 areas by grouping some et together. What part of the garden could eac What information do you need to use?	ns. She will fence equal sections h fenced area be?
b. c.	How can writing an equation help you solve How can drawing a model help you write an	the problem?
d.	Show how you can solve the problem.	<ul> <li>e. Complete the sentence.</li> <li>The garden can be fenced into,</li> <li>, and parts or,</li> <li>, and parts.</li> </ul>
10.	What is $\frac{7}{10}$ written as a sum of unit fractions?	<b>11. Test Prep</b> Which is equivalent to $\frac{9}{12}$ ? (A) $\frac{5}{12} + \frac{3}{12}$ (B) $\frac{3}{12} + \frac{2}{12} + \frac{1}{12} + \frac{1}{12}$ (C) $\frac{5}{12} + \frac{2}{12} + \frac{2}{12}$ (D) $\frac{4}{12} + \frac{4}{12} + \frac{1}{12} + \frac{1}{12}$

## Add Fractions Using Models

**Essential Question** How can you add fractions with like denominators using models?



**1. Explain** how the numerator of the sum is related to the fraction strip model.



**2. Explain** how the denominator of the sum is related to the fraction strip model.

## 🚹 Example

Jacob needs two strips of wood to make masts for a miniature sailboat. One mast will be  $\frac{3}{6}$  foot long. The other mast will be  $\frac{2}{6}$  foot long. He has a strip of wood that is  $\frac{4}{6}$  foot long. Is this strip of wood long enough to make both masts?



- **3. Explain** how you used the number line to determine if the sum was less than  $\frac{4}{6}$ .
- **4.** What if each mast was  $\frac{2}{6}$  foot long? Could Jacob use the strip of wood to make both masts? Explain.

## Share and Show MATH

1. Gary's cat ate  $\frac{3}{5}$  of a bag of cat treats in September and  $\frac{1}{5}$  of the same bag of cat treats in October. What part of the bag of cat treats did Gary's cat eat in both months?

Use the model to find the sum  $\frac{3}{5} + \frac{1}{5}$ .

How many fifth-size pieces are shown? \_\_\_\_

$$\frac{3}{5} + \frac{1}{5} = \frac{1}{5}$$
 of a bag



Use the model to find the sum.





Find the sum. Use models to help.



## On Your Own **Explain** how to add $\frac{2}{6} + \frac{3}{6}$

Find the sum. Use models to help.



13. Write Math Jin is putting colored sand in a jar. She filled  $\frac{2}{10}$  of the jar with blue sand and  $\frac{4}{10}$  of the jar with pink sand. Describe one way to model the part of the jar filled with sand.



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**15.** Test Prep Rita needs  $\frac{4}{8}$  yard of ribbon to wrap a gift for her sister and  $\frac{2}{8}$  yard of ribbon to wrap a gift for a friend. How much ribbon does she need to wrap both gifts?











## Connect to Art

#### **Stained Glass Windows**

Have you ever seen a stained glass window in a building or home? Artists have been designing stained glass windows for thousands of years.

Help design the stained glass sail on the boat below.

**Materials** color pencils Look at the eight triangles in the sail. Use the guide below to color the triangles:

- $\frac{2}{8}$  blue
- $\frac{3}{8}$  red
- $\frac{2}{8}$  orange
- $\frac{1}{8}$  yellow
- **16.** Write an equation that shows the fraction of triangles that are red or blue.
- 17. What part of the sail is orange or yellow?Explain how you found the answer.

- **18.** What color is the greatest part of the sail? Write a fraction for that color. How do you know that fraction is greater than the other fractions? **Explain.**
- **19.** Write Math Pose a Problem Write a problem about the sail that uses addition of fractions.





## **Subtract Fractions Using Models**

**Essential Question** How can you subtract fractions with like denominators using models?

**UNLOCK** the Problem REAL WORLD

A rover needs to travel  $\frac{5}{8}$  mile to reach its destination. It has already traveled  $\frac{3}{8}$  mile. How much farther does the rover need to travel?

Compare fractions to find the difference.

**STEP 1** Shade the model.

Shade the model to show the total distance.

Then shade the model to show how much distance the rover has already covered.





**STEP 2** Write the difference.

$$\frac{5}{8} - \frac{3}{8} = \frac{1}{8}$$

So, the rover needs to travel \_\_\_\_\_ mile farther.

**1. Explain** how the model shows how much farther the rover needs to travel.



**3. Explain** how the equation  $\frac{6}{6} - \frac{2}{6} = \frac{4}{6}$  is related to the problem situation.

4. Explain how you could find the unknown addend in  $\frac{2}{6} + \blacksquare = 1$  without using a model.

# Share and Show MATH

**1.** Lisa needs  $\frac{4}{5}$  pound of shrimp to make shrimp salad. She has  $\frac{1}{5}$  pound of shrimp. How much more shrimp does Lisa need to make the salad?

Subtract  $\frac{4}{5} - \frac{1}{5}$ . Use the model to help.

Shade the model to show how much shrimp Lisa needs.

Then shade the model to show how much shrimp Lisa has. Compare the difference between the two shaded rows.

$$\frac{4}{5} - \frac{1}{5} = \frac{1}{5}$$
 pound

Lisa needs \_\_\_\_\_ pound more shrimp.

#### Use the model to find the difference.



#### Subtract. Use models to help.



# On Your Own Subtract. Use models to help. 7. $\frac{2}{3} - \frac{1}{3} =$ 10. $\frac{2}{4} - \frac{1}{4} =$ 11. $\frac{9}{10} -$ 13. $\frac{6}{8} - \frac{5}{8} =$

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**8.** 
$$\frac{7}{8} - \frac{5}{8} =$$
 \_\_\_\_\_  
**1.**  $\frac{9}{10} - \frac{3}{10} =$ 

**14.** 
$$1 - \frac{1}{3} =$$
\_\_\_\_\_

#### MATHEMATICAL PRACTICES

Math Talk Explain why the numerator changes when you subtract fractions with like denominators, but the denominator doesn't.

9. 
$$\frac{4}{12} - \frac{2}{12} =$$
 \_\_\_\_\_  
12.  $1 - \frac{5}{8} =$  \_\_\_\_\_  
15.  $\frac{4}{5} - \frac{2}{5} =$ 



## **Add and Subtract Fractions**

**Essential Question** How can you add and subtract fractions with like denominators?

Julie is making a poster for a book report. The directions say to use  $\frac{1}{5}$  of the poster to describe the setting,  $\frac{2}{5}$  of the poster to describe the characters, and the rest of the poster to describe the plot. What part of the poster will she use to describe the plot?

## **Example** Use a model.

Shade \_\_\_\_\_\_ to represent the part for the setting.

Shade \_\_\_\_\_\_ to represent the part for the characters.

		1		
<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>
5	5	5	5	5

• Write an equation for the part of the poster used for

the setting and characters.

- What does the part of the model that is not shaded represent?
- Write an equation for the part of the poster she will use for the plot.

So, Julie will use	of the poster to describe the plot.	Mati he	Talk Why should Julie divide r poster into 5 equal parts
		ins	stead of 3 equal parts? Explain.
1. What's the Error? Lu	lke says $\frac{1}{5} + \frac{2}{5} = \frac{3}{10}$ . <b>Describe</b> his er	ror.	

Setting

Characters

Plot

**Common Denominators** Fractions with common denominators represent wholes divided into the same number of equal-size parts. To add or subtract fractions with the same denominator, you can add or subtract the number of parts given in the numerators.

## **Example** Complete each equation.

Words	Fractions
1 fourth-size part + 2 fourth-size parts = fourth-size parts	$\frac{1}{4} + \frac{2}{4} = \frac{1}{4}$
3 sixth-size parts + 2 sixth-size parts =	$\frac{3}{6} + \frac{2}{6} =$
7 tenth-size parts – 4 tenth-size parts =	

 Sense or Nonsense? Brian says that when you add or subtract fractions with the same denominator, you can add or subtract the numerators and keep the same denominator. Is Brian correct? Explain.



## On Your Own

Find the sum or difference.

8. 
$$\frac{1}{2} + \frac{1}{2} =$$
 9.  $\frac{5}{6} - \frac{4}{6} =$ 
 10.  $\frac{4}{5} - \frac{2}{5} =$ 

 11.  $\frac{1}{10} + \frac{3}{10} =$ 
 12.  $\frac{5}{12} - \frac{1}{12} =$ 
 13.  $\frac{3}{8} + \frac{2}{8} =$ 

#### Practice: Copy and Solve Find the sum or difference.





20. Write Math A city worker is painting a stripe down the center of Main Street. Main Street is  $\frac{8}{10}$  mile long. The worker painted  $\frac{4}{10}$  mile of the street. Explain how to find what part of a mile is left to paint.

- **21.** The length of a rope was  $\frac{6}{8}$  yard. Jeff cut the rope into 3 pieces. Each piece is a different length measured in eighths of a yard. What is the length of each piece of rope?
- **22.** Test Prep Otis has 1 cup of granola. He added  $\frac{3}{8}$  cup to a bowl of yogurt. How much granola is left?



**16.** 
$$\frac{1}{12} + \frac{7}{12} =$$

**19.** 
$$\frac{4}{5} - \_\_\_= \frac{1}{5}$$



## Problem Solving REAL WORLD

#### **Sense or Nonsense?**

**23.** Harry says that  $\frac{1}{4} + \frac{1}{8} = \frac{2}{8}$ . Jane says  $\frac{1}{4} + \frac{1}{8} = \frac{3}{8}$ . Whose answer makes sense? Whose answer is nonsense? **Explain** your reasoning. Draw a model to help.







Name .



## ► Vocabulary

Choose the best term from the box.

- 1. A \_\_\_\_\_\_ always has a numerator of 1. (p. 271)
- 2. A number that names part of a whole is a

Vocabulary
fraction
simplest form
unit fraction

## Check Concepts

Write the fraction as a sum of unit fractions.

**3.** 
$$\frac{3}{10} =$$
 \_\_\_\_\_

Use the model to write an equation.



**4.** 
$$\frac{6}{6} =$$
 \_\_\_\_\_

6.				1	
	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6	<u>1</u> 6

Use the model to solve the equation.



8. 
$$\frac{4}{10} + \frac{5}{10} =$$

$$\frac{1}{\frac{1}{10} \frac{1}{10} \frac{1}$$



Fill in the bubble completely to show your answer.

- **15.** Tyrone mixed  $\frac{7}{12}$  quart of red paint with  $\frac{1}{12}$  quart of yellow paint. How much paint does Tyrone have in the mixture?
  - (A)  $\frac{8}{24}$  quart (B)  $\frac{6}{12}$  quart (C)  $\frac{8}{12}$  quart (D)  $\frac{12}{12}$  quart
- **16.** Jorge lives  $\frac{6}{8}$  mile from school and  $\frac{2}{8}$  mile from a ballpark. How much farther does Jorge live from school than from the ballpark?
  - (A)  $\frac{4}{16}$  mile (B)  $\frac{4}{8}$  mile (C)  $\frac{8}{8}$  mile
  - D 8 miles
- **17.** Su Ling started an art project with 1 yard of felt. She used  $\frac{5}{6}$  yard. How much felt does Su Ling have left?

$$\widehat{\mathbf{A}} \frac{1}{6}$$
 yard

**B** 
$$\frac{4}{6}$$
 yard

$$\widehat{\mathbf{C}} \frac{5}{6}$$
 yard

- $\textcircled{D} \, \frac{6}{6} \, \text{yard}$
- **18.** Eloise hung artwork on  $\frac{2}{5}$  of a bulletin board. She hung math papers on  $\frac{1}{5}$  of the same bulletin board. What part of the bulletin board has artwork or math papers?

(A) 
$$\frac{1}{10}$$
  
(B)  $\frac{1}{5}$   
(C)  $\frac{3}{10}$   
(D)  $\frac{3}{5}$ 

## **Rename Fractions and Mixed Numbers**

**Essential Question** How can you rename mixed numbers as fractions greater than 1 and rename fractions greater than 1 as mixed numbers?

# **WILOCK the Problem**

Mr. Fox has  $2\frac{3}{6}$  loaves of corn bread. Each loaf was cut into  $\frac{1}{6}$ -size pieces. If he has 14 people over for dinner, is there enough bread for each person to have 1 piece?

A **mixed number** is a number represented by a whole number and a fraction. You can write a mixed number as a fraction.

To find how many  $\frac{1}{6}$ -size pieces are in  $2\frac{3}{6}$ , write  $2\frac{3}{6}$  as a fraction.

- What is the size of 1 piece of bread relative to the whole?
- How much bread does Mr. Fox need for 14 people?







## Problem Solving REAL WORLD

Use the recipe to solve 17–19.

- **17.** Cal is making energy squares. How many  $\frac{1}{2}$  cups of peanut butter are used in the recipe?
- **18.** What is the amount of bran cereal, written as a fraction greater than 1, that is used in the recipe?



SHOW YOUR WORK

- 19. Suppose Cal wants to make 2 times as many energy squares as the recipe makes. How many cups of bran cereal should he use? Write your answer as a mixed number and as a fraction greater than 1 in simplest form.
- **20.** Cal added  $2\frac{3}{8}$  cups of raisins. Write this mixed number as a fraction greater than 1 in simplest form.
- 21. Jenn is preparing brown rice. She needs  $1\frac{1}{2}$  cups of brown rice and 2 cups of water. Jenn has only a  $\frac{1}{8}$ -cup measuring cup. How many  $\frac{1}{8}$  cups each of rice and water will Jenn use to prepare the rice?
- **22.** Test Prep Which fraction greater than 1 can you write for  $4\frac{5}{9}$ ?



**Essential Question** How can you add and subtract mixed numbers with like denominators?



After a party, there were  $1\frac{4}{6}$  quesadillas left on one tray and  $2\frac{3}{6}$  quesadillas left on another tray. How much of the quesadillas were left?

• What operation will you use?

• Is the sum of the fractional parts of the mixed numbers greater than 1?

Lesson 7.7



## **Example** Subtract mixed numbers.

Alejandro had  $3\frac{4}{6}$  quesadillas. His family ate  $2\frac{3}{6}$  of the quesadillas. How many quesadillas are left?

Find  $3\frac{4}{6} - 2\frac{3}{6}$ .

#### MODEL

Shade the model to show  $3\frac{4}{6}$ .

Then cross out  $2\frac{3}{6}$  to model the subtraction.



#### RECORD

Subtract the fractional parts of the mixed numbers.

Then subtract the whole-number parts of the mixed numbers.





So, there are \_\_\_\_\_ quesadillas left.

## Share and Show

# Write the sum as a mixed number with the fractional part less than 1.



Find the difference.



## **On Your Own**.

Write the sum as a mixed number with the fractional part less than 1.



Find the difference.



Practice: Copy and Solve Find the sum or difference.

 $\begin{array}{ll} \text{Practice: Cop}\\ \text{I15. } 1\frac{3}{8}+2\frac{7}{8}\\ \text{I8. } 6\frac{3}{5}+4\frac{3}{5}\\ \end{array}$ **16.**  $6\frac{5}{8} - 4$ **17.**  $9\frac{1}{2} + 8\frac{1}{2}$ **20.**  $7\frac{3}{5} - 6\frac{3}{5}$ **19.**  $8\frac{7}{10} - \frac{4}{10}$ 

## Problem Solving REAL WORLD

#### Solve. Write your answer as a mixed number.

- **21.** The driving distance from Alex's house to the museum is  $6\frac{7}{10}$  miles. What is the round-trip distance?
- 22. The driving distance from the sports arena to Kristina's house is  $10\frac{9}{10}$  miles. The distance from the sports arena to Luke's house is  $2\frac{7}{10}$  miles. How much greater is the driving distance between the sports arena and Kristina's house than between the sports arena and Luke's house?
- **23.** Benji biked from his house to the nature preserve, a distance of  $23\frac{4}{5}$  miles. Jade biked from her house to the lake, a distance of  $12\frac{2}{5}$  miles. How many fewer miles did Jade bike than Benji?
- **24.** During the Samson family trip, they drove from home to a ski lodge, a distance of  $55\frac{4}{5}$  miles, and then drove an additional  $12\frac{4}{5}$  miles to visit friends. If the family drove the same route back home, what was the distance traveled during their trip?
- **25.** Test Prep Jeff used  $4\frac{7}{8}$  cups of orange juice and  $3\frac{1}{8}$  cups of pineapple juice to make tropical punch. How much more orange juice than pineapple juice did Jeff use?

(A) 
$$\frac{3}{4}$$
 cup

**B** 
$$1\frac{3}{4}$$
 cups

$$\bigcirc 1\frac{7}{8}$$
 cups



## Subtraction with Renaming

**Essential Question** How can you rename a mixed number to help you subtract?

**WILOCK the Problem** 

Bruce, Chandler, and Chase go bike riding on weekends. On one weekend, Chase rode his bike for 3 hours, Chandler rode her bike for  $2\frac{1}{4}$ hours, and Bruce rode his bike for  $1\frac{3}{4}$  hours. How much longer did Chandler ride her bike than Bruce did?

- Which operation will you use?
- In the problem, circle the numbers that you need to use to find a solution.

Use a model. Find  $2\frac{1}{4} - 1\frac{3}{4}$ .

Shade the model to show how long Chandler rode her bike. Then shade the model to show how long Bruce rode his bike.



- So, Chandler rode her bike \_\_\_\_\_ hour longer than Bruce did.
- **1.** If you have 1 fourth-size part, can you take away 3 fourth-size parts? **Explain.**
- **2.** If you have 1 whole and 1 fourth-size part, can you take away 3 fourth-size parts? **Explain**.

## **One Way** Rename the first mixed number.

Find the difference.  $5\frac{1}{8} - 3\frac{3}{8}$ 

#### **STEP** 1

Rename  $5\frac{1}{8}$  as a mixed number with a fraction greater than 1.



#### **STEP 2**

Subtract the mixed numbers.



## **Another Way** Rename both mixed numbers.

Find the difference.  $3\frac{4}{12} - 1\frac{6}{12}$ 

**STEP** 1

Rename both mixed numbers as fractions greater than 1.

$$3\frac{4}{12} = \frac{1}{12}$$
  $1\frac{6}{12} = \frac{1}{12}$ 

STEP 2

Subtract the fractions greater than 1.



• Explain how you could rename 5 to subtract  $3\frac{1}{4}$ .

MATHEMATICAL PRACTICES

need to rename  $5\frac{1}{8}$ .

Name \_

## Share and Show MATH

**1.** Rename both mixed numbers as fractions. Find the difference.



#### Find the difference.



## **On Your Own**

#### Find the difference.



## Practice: Copy and Solve Find the difference.

8.  $4\frac{1}{6} - 2\frac{5}{6}$ 9.  $6\frac{9}{12} - 3\frac{10}{12}$ 10.  $3\frac{3}{10} - \frac{7}{10}$ 11.  $4 - 2\frac{3}{5}$ 12.  $5\frac{1}{4} - 2\frac{3}{4}$ 13.  $3\frac{9}{12} - 1\frac{11}{12}$ 14.  $7\frac{3}{10} - 4\frac{7}{10}$ 15.  $2\frac{3}{8} - 1\frac{5}{8}$ 

## Problem Solving REAL WORLD

#### Rename the fractions to solve.

Many instruments are coiled or curved so that they are easier for the musician to play, but they would be quite long if straightened out completely.

- **16.** Trumpets and cornets are brass instruments. Fully stretched out, the length of a trumpet is  $5\frac{1}{4}$  feet and the length of a cornet is  $4\frac{2}{4}$  feet. The trumpet is how much longer than the cornet?
- **17.** Bassoons and double bassoons are woodwind instruments. Fully stretched out, the length of a bassoon is  $9\frac{2}{12}$  feet and the length of a double bassoon is  $18\frac{1}{12}$  feet. The double bassoon is how much longer than the bassoon?
- **18.** Tubas, trombones, and French horns are brass instruments. Fully stretched out, the length of a tuba is 18 feet, the length of a trombone is  $9\frac{11}{12}$  feet, and the length of a French horn is  $17\frac{1}{12}$  feet. The tuba is how much longer than the French horn? The French horn is how much longer than the trombone?
- **19.** The pitch of a musical instrument is related to its length. In general, the greater the length of a musical instrument, the lower its pitch. Order the brass instruments identified on this page from lowest pitch to the highest pitch.
- **20.** Test Prep Sam ran  $2\frac{2}{5}$  miles on Saturday and  $1\frac{4}{5}$  miles on Monday. How many more miles did Sam run on Saturday than on Monday?



300 FOR MORE PRACTICE: Standards Practice Book, pp. P147–P148 

## **Fractions and Properties of Addition**

Essential Question How can you add fractions with like denominators using the properties of addition?

**CONNECT** The Associative and Commutative Properties of Addition can help you group and order addends to find sums mentally. You can use mental math to combine fractions that have a sum of 1.

- The Commutative Property of Addition states that when the order of two addends is changed, the sum is the same. For example, 4 + 5 = 5 + 4.
- The Associative Property of Addition states that when the grouping of addends is changed, the sum is the same. For example, (5 + 8) + 4 = 5 + (8 + 4).

## **UNLOCK** the Problem **TREAL**

The map shows four lighthouses in the Florida Keys and their distances apart in miles. The Dry Tortugas Lighthouse is the farthest west, and the Alligator Reef Lighthouse is the farthest east.

What is the distance from the Dry Tortugas Lighthouse to the Alligator Reef Lighthouse, traveling between the four lighthouses?

Use the properties to order and group. Add.  $70\frac{5}{10} + 43\frac{6}{10} + 34\frac{5}{10}$ 





WORLD

Property to order the addends so that the fractions with a sum of 1 are together.

Use the Commutative

Use the Associative Property to group the addends that you can add mentally.

Sombrero

Key Lighthouse

Add the grouped numbers, and then add the other mixed number.

Write the sum.

So, the distance from the Dry Tortugas Lighthouse to the Alligator Reef Lighthouse, traveling between the four lighthouses, is

miles.



Key West

Lighthouse

 $70\frac{5}{10}$ 

Dry Tortugas Lighthouse





**Try This!** Use the properties and mental math to solve. Show each step, and name the property used.



# Share and Show MATH

**1.** Complete. Name the property used.

$$\left( 3\frac{4}{10} + 5\frac{2}{10} \right) + \frac{6}{10} = \left( 5\frac{2}{10} + 3\frac{4}{10} \right) + \_\_\_\_= 5\frac{2}{10} + \left( 3\frac{4}{10} + \_\_\_\right) = 5\frac{2}{10} + \_\_\_= 5\frac{2}{10} + \_\_= 5\frac{2}{10} + \_\_\_= 5\frac{2}{10} + \_\_= 5\frac{2}{10} + \_\_\_= 5\frac{2}{10} + \_\_= 5\frac{2}{10} + \_\_\_= 5\frac{2}{10} + \_\_= 5\frac{2}{10} + \_= 5\frac{2}{10}$$

	MATHEMATICAL PRACTICES
Math Talk	Describe how you
could use	the properties to
find the s	um $1\frac{1}{3} + 2\frac{5}{8} + 1\frac{2}{3}$ .

Use the properties and mental math to find the sum.

2. 
$$\left(2\frac{7}{8}+3\frac{2}{8}\right)+1\frac{1}{8}$$
  
3.  $1\frac{2}{5}+\left(1+\frac{3}{5}\right)$   
4.  $5\frac{3}{6}+\left(5\frac{5}{6}+4\frac{3}{6}\right)$   
5.  $\left(1\frac{1}{4}+1\frac{1}{4}\right)+2\frac{3}{4}$   
6.  $\left(12\frac{4}{9}+1\frac{2}{9}\right)+3\frac{5}{9}$   
6.  $\left(12\frac{4}{9}+1\frac{2}{9}\right)+3\frac{5}{9}$   
6.  $\left(12\frac{4}{9}+1\frac{2}{9}\right)+3\frac{5}{9}$ 

Name \_

## On Your Own.....

Use the properties and mental math to find the sum.

8. 
$$\left(45\frac{1}{3}+6\frac{1}{3}\right)+38\frac{2}{3}$$
  
9.  $\frac{1}{2}+\left(103\frac{1}{2}+12\right)$   
10.  $\left(3\frac{5}{10}+10\right)+11\frac{5}{10}$   
11.  $1\frac{4}{10}+\left(37\frac{3}{10}+\frac{6}{10}\right)$   
12.  $\left(\frac{3}{12}+10\frac{5}{12}\right)+\frac{9}{12}$   
13.  $5\frac{7}{8}+\left(6\frac{3}{8}+\frac{1}{8}\right)$ 

#### Use the expressions in the box for 14-15.

- **14.** Which property of addition would be best to solve Expression A?
- **15.** Which two expressions have the same value?
- **16.** Test Prep Shari represented the perimeter of a triangle she measured using the expression  $1\frac{1}{2} + (2 + 2\frac{1}{2})$ . How could Shari rewrite the expression using both the Associative and Commutative Properties?

Α	$\frac{1}{8} + \left(\frac{7}{8} + \frac{4}{8}\right)$
В	$\frac{1}{2} + 2$
С	$\frac{3}{7} + \left(\frac{1}{2} + \frac{4}{7}\right)$
D	$\frac{1}{3} + \frac{4}{3} + \frac{2}{3}$

MATICAL Model • Reason • Make Sense

## Problem Solving REAL WORLD

#### Pose a Problem

17. Costumes are being made for the high school musical. The table at the right shows the amount of fabric needed for the costumes of the male and female leads. Alice uses the expression  $7\frac{3}{8} + 1\frac{5}{8} + 2\frac{4}{8}$  to find the total amount of fabric needed for the costume of the female lead.

To find the value of the expression using mental math, Alice used the properties of addition.

$$7\frac{3}{8} + 1\frac{5}{8} + 2\frac{4}{8} = \left(7\frac{3}{8} + 1\frac{5}{8}\right) + 2\frac{4}{8}$$

Alice added 7 + 1 and was able to quickly add  $\frac{3}{8}$  and  $\frac{5}{8}$  to the sum of 8 to get 9. She added  $2\frac{4}{8}$  to 9, so her answer was  $11\frac{4}{8}$ .

So, the amount of fabric needed for the costume of the female lead actor is  $11\frac{4}{8}$  yards.

Write a new problem using the information for the costume for the male lead actor.

	Pose a Problem	
(		1

• Explain how using the properties of addition makes both problems easier to solve.

	*	×
Costur	me Fabric (	in Yards)
Material	Female Lead Costume	Male Lead Costume
Silk	7 <mark>3</mark>	$1\frac{2}{8}$
Felt	1 <mark>5</mark>	2 <mark>3</mark> 8
Cotton	$2\frac{4}{8}$	5 <mark>6</mark> 8
	0	8

#### Solve your problem. Check your solution.

#### Name \_

## **Problem Solving • Multistep Fraction** Problems

Essential Question How can you use the strategy act it out to solve multistep problems with fractions?

UNLOCK the Problem REAL WORLD

A gift shop sells walnuts in  $\frac{3}{4}$ -pound bags. Ann will buy some bags of walnuts and repackage them into 1-pound bags. What is the least number of  $\frac{3}{4}$ -pound bags Ann could buy, if she wants to fill each 1-pound bag, without leftovers?



#### **Solve the Problem Read the Problem** What do I need to find? Describe how to act it out. Use fraction circles. One $\frac{3}{4}$ -pound bag Not enough for a 1-pound bag I need to find how many bags of walnuts Ann needs to make 1-pound $\frac{1}{4}$ bags of walnuts, without leftovers. $\frac{3}{4} = \frac{3}{4}$ What information do I need Two $\frac{3}{4}$ -pound bags One 1-pound bag with to use? $\frac{2}{4}$ pound left over The bags she will buy contain $\frac{1}{4}$ pound of walnuts. She 3 + 3 =<u>1</u> 4 will repackage the walnuts into 6 -pound bags. Three $\frac{3}{4}$ -pound bags have $\frac{3}{4} + \frac{3}{4} + \frac{3}{4} = \frac{1}{4}$ pounds of How will I use the walnuts. This makes \_\_\_\_\_ 1-pound bags with \_\_\_\_\_ information? pound left over. I can use fraction circles to Four $\frac{3}{4}$ -pound bags have $\frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4} = -$ \_\_\_\_\_-pounds the problem. of walnuts. This makes \_\_\_\_\_ 1-pound bags with \_\_\_\_\_ left over.

So, Ann could buy <u> $\frac{3}{4}$ </u>-pound bags of walnuts.

## Try Another Problem

At the end of dinner, a restaurant had several dishes of quiche, each with 2 sixth-size pieces of quiche. The chef was able to combine these pieces to make 2 whole quiches, with no leftovers. How many dishes did the chef combine?



Read the Problem	Solve the Problem
What do I need to find?	Describe how to act it out.
What information do I need to use?	
How will I use the information?	

So, the chef combined \_\_\_\_\_ dishes each with  $\frac{2}{6}$  quiche.



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#### Tips **UNLOCK** the Problem

Underline the question.

Circle the important facts.

Cross out unneeded information.

ATHEMATICAL Model • Reason • Make Sense

## On Your Own . . .

- **5.** A company shipped 15,325 boxes of apples and 12,980 boxes of oranges. How many more boxes of apples than oranges did the company ship?
- **6.** A fair sold a total of 3,300 tickets on Friday and Saturday. It sold 100 more on Friday than on Saturday. How many tickets did the fair sell on Friday?
- 7. Write Math Emma walked  $\frac{1}{4}$  mile on Monday,  $\frac{2}{4}$  mile on Tuesday, and  $\frac{3}{4}$  mile on Wednesday. If the pattern continues, how many miles will she walk on Friday? Explain how you found the number of miles.

## Choose a STRATEGY Act It Out

Draw a Diagram Find a Pattern Make a Table or List Solve a Simpler Problem

#### SHOW YOUR WORK

- 8. Jared painted a mug  $\frac{5}{12}$  red and  $\frac{4}{12}$  blue. What part of the mug is **not** red or blue?
- **9.** Test Prep Sophia spent  $\frac{3}{4}$  hour reading about the Warwick Applefest. Then she spent  $\frac{1}{4}$  hour writing a paragraph about the festival. How long did Sophia spend reading and writing about the festival?
  - (A)  $\frac{1}{4}$  hour (B)  $\frac{2}{4}$  hour
- C 1 hour

**(D)** 
$$1\frac{1}{4}$$
 hours

Name .



## Vocabulary

Choose the best term from the box.

1. A number represented by a whole number and a fraction is a

\_\_\_\_. (p. 289)

2. A fraction that always has a numerator of 1 is a

\_\_\_\_\_. (p. 271)

## Check Concepts

Write the fraction as a sum of unit fractions.

**3.**  $\frac{4}{5} =$ 

**4.** 
$$\frac{5}{10}$$

Write the mixed number as a fraction.  
5. 
$$1\frac{3}{9} =$$
 6.  $4\frac{2}{2} =$ 

**5.** 
$$1\frac{3}{8} =$$

8.  $\frac{12}{10}$ 

Write the fraction as a mixed number.

Find the sum or difference.

**9.**  $\frac{10}{3} =$ 

**10.**  $\frac{15}{6} =$ 

**13.** 
$$5\frac{7}{10} - 4\frac{5}{10} =$$
\_\_\_\_\_  
**16.**  $\frac{4}{12} + \frac{6}{12} =$ \_\_\_\_\_

**7.**  $2\frac{3}{5} =$ 

Use the properties and mental math to find the sum.

**11.**  $2\frac{3}{8} + 1\frac{6}{8} =$  **12.**  $\frac{9}{12} - \frac{2}{12} =$  **14.**  $4\frac{1}{6} - 2\frac{5}{6} =$  **15.**  $3\frac{2}{5} - 1\frac{4}{5} =$ 



**19.** 
$$\frac{3}{10} + \left(2\frac{4}{10} + \frac{7}{10}\right)$$



Company Company Company

Vocabulary	
mixed number	
simplest form	
unit fraction	

Fill in the bubble completely to show your answer.

- **20.** Eddie cut  $2\frac{2}{4}$  feet of balsa wood for the length of a kite. He cut  $\frac{3}{4}$  foot for the width of the kite. How much longer is the length of the kite than the width?
  - (A)  $1\frac{1}{4}$  feet (B)  $1\frac{3}{4}$  feet (C) 2 feet (D)  $3\frac{1}{4}$  feet
- **21.** On a trip to the art museum, Lily rode the subway for  $\frac{7}{10}$  mile and walked for  $\frac{3}{10}$  mile. How much farther did she ride on the subway than walk?
  - (A)  $\frac{3}{10}$  mile (B)  $\frac{4}{10}$  mile (C)  $\frac{7}{10}$  mile (D) 1 mile
- **22.** Pablo is training for a marathon. He ran  $5\frac{4}{8}$  miles on Friday,  $6\frac{5}{8}$  miles on Saturday, and  $7\frac{4}{8}$  miles on Sunday. How many miles did he run on all three days ?
  - (A)  $1\frac{5}{8}$  miles
  - (B)  $12\frac{1}{8}$  miles
  - $\bigcirc 19\frac{4}{8}$  miles
  - (D)  $19\frac{5}{8}$  miles
- 23. Cindy has two jars of paint.



Which fraction below represents how much paint Cindy has?



- **24.** Cole grew  $2\frac{3}{4}$  inches last year. Kelly grew the same amount. Which fraction below represents the number of inches that Kelly grew last year?
  - $\textcircled{A}\frac{3}{4}$
  - $\mathbb{B} \frac{5}{4}$
  - $\bigcirc \frac{11}{4}$

  - (D)  $\frac{14}{4}$
- **25.** Olivia's dog is 4 years old. Her cat is  $1\frac{1}{2}$  years younger. How old is Olivia's cat?
  - (A)  $5\frac{1}{2}$  years old **(B)**  $3\frac{1}{2}$  years old
  - $\bigcirc 2\frac{1}{2}$  years old **(D)**  $1\frac{1}{2}$  years old
- **26.** Lisa mixed  $4\frac{4}{6}$  cups of orange juice with  $3\frac{1}{6}$  cups of milk to make a health shake. She drank  $3\frac{3}{6}$  cups of the health shake. How much of the health shake did Lisa not drink?
  - $(\mathbf{A}) \frac{2}{6}$  cups **(B)**  $4\frac{2}{6}$  cups  $\bigcirc$  7 $\frac{5}{6}$  cups
  - (D)  $11\frac{2}{6}$  cups
- 27. Keiko entered a contest to design a new school flag. Five twelfths of her flag has stars and  $\frac{3}{12}$  has stripes. What fraction of Keiko's flag has stars and stripes?
  - **A**  $\frac{8}{12}$  $\textcircled{B}\frac{8}{24}$  $\bigcirc \frac{2}{12}$ (D)  $\frac{2}{24}$

## Constructed Response

**28.** Ela is knitting a scarf from a pattern. The pattern calls for  $4\frac{2}{12}$  yards of yarn. She has only  $2\frac{11}{12}$  yards of yarn. How much more yarn does Ela need to finish knitting the scarf? **Explain** how you found your answer.

## Performance Task

- **29.** Miguel's class went to the state fair. The fairground is divided into sections. Rides are in  $\frac{6}{10}$  of the fairground. Games are in  $\frac{2}{10}$  of the fairground. Farm exhibits are in  $\frac{1}{10}$  of the fairground.
- A How much greater is the fraction of the fairground with rides than the fraction with farm exhibits? Draw a model to prove your answer is correct.

- B What fraction of the fairground has games and farm exhibits? Write an equation to show your answer.
- G The rest of the fairground is refreshment booths. What fraction of the fairground is refreshment booths? **Describe** the steps you follow to solve the problem.