# Fractions and 

 DectmalsDeveloping an understanding of fraction equivalence, addition and subtraction of fractions with like denominators, and multiplication of fractions by whole numbers

## Project

## Building Custom Guitars

Do you play the guitar, or would you like to learn how to play one? The guitar size you need depends on your height to the nearest inch and on scale length. Scale length is the distance from the bridge of the guitar to the nut.

## Get Started

Order the guitar sizes from the least size to the greatest size, and complete the table.

## Important Facts

| Guitar Sizes for Students |  |  |  |
| :---: | :---: | :---: | :---: |
| Age of Player | Height of Player <br> (to nearest inch)Scale Length <br> (shortest to longest, in inches) | Size of Guitar |  |
| $4-6$ | 3 feet 3 inches to 3 feet <br> 9 inches | 19 |  |
| $6-8$ | 3 feet 10 inches to 4 feet <br> 5 inches | 20.5 |  |
| $8-11$ | 4 feet 6 inches to 4 feet <br> 11 inches | 22.75 |  |
| 11-Adult | 5 feet or taller | 25.5 |  |

Size of Guitar: $\frac{1}{2}$ size, $\frac{4}{4}$ size, $\frac{1}{4}$ size, $\frac{3}{4}$ size

Adults play $\frac{4}{4}$-size guitars. You can see that guitars also come in $\frac{3}{4}, \frac{1}{2}$, and $\frac{1}{4}$ sizes. Figure out which size guitar you would need according to your height and the scale length for each size guitar. Use the Important Facts to decide. Explain your thinking.


# Fraction Equivalence and comparison 

## Show What You Know

Check your understanding of important skills.
Name $\qquad$
Part of a Whole Write a fraction for the shaded part.
1.

2.

3.


Name the Shaded Part Write a fraction for the shaded part.
4.

5.

6.


Compare Parts of a Whole Color the fraction strips to show the fractions. Circle the greater fraction.


Earth's surface is covered by more than 57 million square miles of land. The table shows about how much of Earth's land surface each continent covers. Be a Math Detective. Which continent covers the greatest part of Earth's land surface?


| Continent | Part of <br> Land Surface |
| :--- | :---: |
| Asia | $\frac{3}{10}$ |
| Africa | $\frac{1}{5}$ |
| Antarctica | $\frac{9}{100}$ |
| Australia | $\frac{6}{100}$ |
| Europe | $\frac{7}{100}$ |
| North America | $\frac{1}{6}$ |
| South America | $\frac{1}{8}$ |

## Vocabulary Builder

## Visualize It

Complete the flow map by using the words with a $\checkmark$.
Whole Numbers and Fractions
What is it?


## Understand Vocabulary

## Complete the sentences by using preview words.

1. A fraction is in $\qquad$ if the numerator and denominator have only 1 as a common factor.
2. $\qquad$ name the same amount.
3. A $\qquad$ is a common multiple of two or more denominators.
4. A $\qquad$ is a known size or amount that helps you understand a different size or amount.
$\qquad$

## Equivalent Fractions

Essential Question How can you use models to show equivalent fractions?

## Investigate

Materials $■$ color pencils Joe cut a pan of brownies into third-size pieces. He kept $\frac{1}{3}$ and gave the rest away. Joe will not eat his part all at once. How can he cut his part into smaller, equal-size pieces?
A. Draw on the model to show how Joe could cut his part of the brownies into 2 equal pieces.


You can rename these 2 equal pieces as a fraction of the original pan of brownies.

Suppose Joe had cut the original pan of brownies into equal pieces of this size.

How many pieces would there be? $\qquad$


What fraction of the pan is 1 piece? $\qquad$
What fraction of the pan is 2 pieces? $\qquad$
You can rename $\frac{1}{3}$ as $\qquad$ .
B. Now draw on the model to show how Joe could cut his part of the brownies into 4 equal pieces.
You can rename these 4 equal pieces as a fraction of the original pan of brownies.

Suppose Joe had cut the original pan of
 brownies into equal pieces of this size.

How many pieces would there be? $\qquad$
What fraction of the pan is 1 piece? $\qquad$
What fraction of the pan is 4 pieces? $\qquad$ You can rename $\frac{1}{3}$ as $\qquad$ .
C. Fractions that name the same amount are equivalent fractions. Write the equivalent fractions.

$$
\frac{1}{3}=\square=\square
$$

## Draw Conclusions

1. Compare the models for $\frac{1}{3}$ and $\frac{2}{6}$. How does the number of parts relate to the sizes of the parts?
$\qquad$
$\qquad$
2. Describe how the numerators are related and how the denominators are related in $\frac{1}{3}=\frac{2}{6}$.
$\qquad$
$\qquad$
$\qquad$
3. A.O.I. Apply Does $\frac{1}{3}=\frac{3}{9}$ ? Explain.

## Make Connections

Savannah has $\frac{2}{4}$ yard of ribbon, and Lin has $\frac{3}{8}$ yard of ribbon.
How can you determine whether Savannah and Lin have the same length of ribbon?

The equal sign ( $=$ ) and not equal to sign $(\neq)$ show whether fractions are equivalent.
Tell whether $\frac{2}{4}$ and $\frac{3}{8}$ are equivalent. Write $=$ or $\neq$.
STEP 1 Shade the amount of ribbon Savannah has.


STEP 2 Shade the amount of ribbon Lin has.

Think: $\frac{2}{4}$ yard is not the same amount as $\frac{3}{8}$ yard.

$\qquad$

## Share and Show

Use the model to write an equivalent fraction.
$\bigcirc 2$.
1.

$\frac{1}{5}$
$\frac{2}{3}$




Tell whether the fractions are equivalent. Write $=$ or $\neq$.
3. $\frac{1}{6} \bigcirc \frac{2}{12}$
4. $\frac{2}{5} \bigcirc \frac{6}{10}$
5. $\frac{4}{12} \bigcirc \frac{1}{3}$
6. $\frac{5}{8} \bigcirc \frac{2}{4}$
7. $\frac{5}{6} \bigcirc \frac{10}{12}$
8. $\frac{1}{2} \bigcirc \frac{5}{10}$
9. Write Math Manny used 8 tenth-size parts to model $\frac{8}{10}$. Ana used fewer parts to model an equivalent fraction. How does the size of a part in Ana's model compare to the size of a tenth-size part? Explain.
$\qquad$
$\qquad$
10. H.O. How many eighth-size parts do you need to model $\frac{3}{4}$ ? Explain.
$\qquad$
$\qquad$
11. Test Prep Which fraction is equivalent to $\frac{3}{5}$ ?
(A) $\frac{6}{8}$
(B) $\frac{5}{3}$
(C) $\frac{5}{10}$
(D) $\frac{6}{10}$

## Problem Solving

## H.O.T. 7 What's the Error?

12. Ben brought two pizzas to a party. He says that since $\frac{1}{4}$ of each pizza is left, the same amount of each pizza is left. What is his error?


Describe Ben's error.
$\qquad$


Draw models of $\mathbf{2}$ pizzas with a different number of equal pieces. Use shading to show $\frac{1}{4}$ of each pizza.
$\qquad$

## Generate Equivalent Fractions

Essential Question How can you use multiplication to find equivalent fractions?

## UNLOCK the Problem REAL wORLD

Patty needs $\frac{3}{4}$ cup of dish soap to make homemade bubble solution. Her measuring cup is divided into eighths. What fraction of the measuring cup should Patty fill with dish soap?

- Is an eighth-size part of a measuring cup bigger or smaller than a fourth-size part?


## (?) Find how many eighths are in $\frac{3}{4}$.

STEP 1 Compare fourths and eighths.

Shade to model $\frac{1}{4}$.
Use fourth-size parts.


Shade to model $\frac{1}{4}$.
Use eighth-size parts.



You needed 2 eighth-size parts to make 1 fourth-size part.
So, you need $\qquad$ eighth-size parts to make 3 fourth-size parts.

So, Patty should fill $\overline{8}$ of the measuring cup with dish soap.

1. Explain why 6 eighth-size parts is the same amount as

MATHEMATICAL PRACTICES know how many eighth-size parts you needed to make 1 fourth-size part? Explain. 3 fourth-size parts.
$\int$ Example Write four fractions that are equivalent to $\frac{1}{2}$.
MODEL

So, $\frac{1}{2}=\frac{2}{4}=\frac{}{6}=\square=\square$.
2. Look at the model that shows $\frac{1}{2}=\frac{3}{6}$. How does the number of parts in the whole affect the number of parts that are shaded? Explain.
$\qquad$
$\qquad$
3. Explain how you can use multiplication to write a fraction that is equivalent to $\frac{3}{5}$.
$\qquad$
$\qquad$
$\qquad$
4. Are $\frac{2}{3}$ and $\frac{6}{8}$ equivalent? Explain.
$\qquad$

## Share and Show

MATH
BOARD

1. Complete the table below.

MODEL


WRITE EQUIVALENT
FRACTIONS

RELATE EQUIVALENT FRACTIONS



$$
\frac{1}{3}=\frac{4}{12}
$$

Write two equivalent fractions.


Math Talk
MATHEMATICAL PRACTICES
Can you multiply the numerator and denominator of a fraction by 0? Explain.
2. $\frac{4}{5}$


$$
\frac{4}{5}=\square=
$$

3. $\frac{2}{4}$

$\frac{2}{4}=\square=$

## On Your Own

Write two equivalent fractions.
4. $\frac{3}{6}$
$\frac{3}{6}=$
5. $\frac{3}{10}$
$\frac{3}{10}=\square=\square$
6. $\frac{2}{5}$

$$
\frac{2}{5}=\square=\square
$$



Tell whether the fractions are equivalent. Write $=$ or $\neq$.
7. $\frac{5}{6} \bigcirc \frac{10}{18}$
8. $\frac{4}{5} \bigcirc \frac{8}{10}$
9. $\frac{1}{5} \bigcirc \frac{4}{10}$
10. $\frac{1}{4} \bigcirc \frac{2}{8}$

## Problem Solving REAL WORLD

Use the recipe for 11-13.
11. How could you use a $\frac{1}{8}$-cup measuring cup to measure the cornstarch?
$\qquad$
$\qquad$
12. How could you use a $\frac{1}{8}$-cup measuring cup to measure the water?
$\qquad$
13. H.O.I. Kim says the amount of flour in the recipe can be expressed as a fraction. Is she correct? Explain.

## Face Paint Recipe

$\frac{2}{8}$ cup cornstarch
1 tablespoon flour
$\frac{9}{12}$ cup light corn syrup
$\frac{1}{4}$ cup water
$\frac{1}{2}$ teaspoon food coloring
14.

Write Math Explain using words how you know a fraction is equivalent to another fraction.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
15. Test Prep Raul needs a piece of rope $\frac{2}{3}$ yard long. Which fraction is equivalent to $\frac{2}{3}$ ?
(A) $\frac{8}{15}$ yard
(C) $\frac{8}{12}$ yard
(B) $\frac{6}{12}$ yard
(D) $\frac{4}{5}$ yard

$$
5
$$ know a fraction is equivalent to another fraction.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
路
$\qquad$

## Simplest Form

Essential Question How can you write a fraction as an equivalent
fraction in simplest form?

## UNLOCK the Problem REAL wORLD

Vicki bought an ice cream cake cut into 6 equal pieces. Vicki, Margo, and Elena each took 2 pieces of the cake home. Vicki says she and each of her friends took $\frac{1}{3}$ of the cake home. Is Vicki correct?

## 1 Activity

Materials $\quad$ color pencils
STEP 1 Use a blue pencil to shade the pieces Vicki took home.

STEP 2 Use a red pencil to shade the pieces Margo took home.

STEP 3 Use a yellow pencil to shade the pieces Elena took home.

- Into how many pieces was the cake cut?
- How many pieces did each girl take?


The cake is divided into $\qquad$ equal-size pieces. The 3 colors on the model show how to combine sixth-size pieces to make
$\qquad$ equal third-size pieces.

So, Vicki is correct. Vicki, Margo, and Elena each took __ of the cake home.

- What if Vicki took 3 pieces of cake home and Elena sizes of the parts are related. took 3 pieces of cake home. How could you combine the pieces to write a fraction that represents the part each friend took home? Explain.

Simplest Form A fraction is in simplest form when you can represent it using as few equal parts of a whole as possible. You need to describe the part you have in equal-size parts. If you can't describe the part you have using fewer parts, then you cannot simplify the fraction.

## P One Way use models to write an equivalent

fraction in simplest form.
MODEL


$$
\frac{6}{10}=\frac{\square}{5}
$$

$$
\frac{6 \div}{10 \div}=\frac{}{5}
$$



$$
\frac{6}{12}=-
$$

$$
\frac{6 \div}{12 \div}=-
$$

To simplify $\frac{6}{10}$, you can combine tenth-size parts into equal groups with 2 parts each.

So, $\frac{6}{10}=\frac{6 \div}{10 \div}=\square$.

## $\left(\right.$ Another Way Use common factors to write $\frac{6}{10}$

in simplest form.
A fraction is in simplest form when 1 is the only factor that the numerator and denominator have in common. The parts of the whole cannot be combined into fewer equal-size parts to show the same fraction.

STEP 1 List the factors of the numerator and denominator. Circle common factors.

Factors of 6: $\qquad$ , $\qquad$ , $\qquad$ ,

Factors of 10 : $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$
STEP 2 Divide the numerator and denominator by a common factor greater than 1.

$$
\frac{6}{10}=\frac{6 \div}{10 \div}=-
$$

Since 1 is the only factor that 3 and 5 have in common, $\qquad$ is written in simplest form.
$\qquad$

## Share and Show

1. Write $\frac{8}{10}$ in simplest form.

$$
\frac{8}{10}=\frac{8 \div}{10 \div}=
$$

Write the fraction in simplest form.
C2. $\frac{6}{12}$

| $\frac{6}{12}$ | 3. $\frac{2}{10}$ |
| :--- | :--- |

4. $\frac{6}{8}$
5. $\frac{4}{6}$

## On Your Own

Write the fraction in simplest form.
6. $\frac{9}{12}$
7. $\frac{4}{8}$
8. $\frac{10}{12}$
9. $\frac{20}{100}$

Tell whether the fraction is in simplest form.
Write yes or no.
10. $\frac{2}{8}$
11. $\frac{9}{12}$
12. $\frac{5}{6}$
13. $\frac{4}{10}$

Tell whether the fractions are equivalent. Write $=$ or $\neq$. Use simplest form to help.
14. $\frac{3}{6} \bigcirc \frac{5}{10}$
15. $\frac{9}{12} \bigcirc \frac{1}{3}$
16. $\frac{3}{12} \bigcirc \frac{2}{4}$
17. $\frac{6}{8} \bigcirc \frac{9}{12}$

## Problem Solving REAL WORLD

## Use the map for 18-19.

18. What fraction of the states in the southwest region share a border with Mexico? Is this fraction in simplest form?
19. H.O.T. What's the Question? $\frac{1}{3}$ of the states in this region are on the Gulf of Mexico.
$\qquad$
$\qquad$
20. Sense or Nonsense? Pete says that to write $\frac{4}{6}$ as $\frac{2}{3}$, you combine pieces, but to write $\frac{4}{6}$ as $\frac{8}{12}$, you break apart pieces. Does this make sense? Explain.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
21. Test Prep Eight of 12 students bought lunch today. In simplest form, what fraction of the students bought lunch today?
(A) $\frac{4}{6}$
(B) $\frac{2}{3}$
(C) $\frac{10}{12}$
(D) $\frac{12}{12}$
$\qquad$

## Common Denominators

Essential Question How can you write a pair of fractions as fractions with a common denominator?

## UNLOCK the Problem REAL wORLD

Martin has two cakes that are the same size. One cake is cut into $\frac{1}{2}$-size pieces. The other cake is cut into $\frac{1}{3}$-size pieces. He wants to cut the cakes so they have the same size pieces. How can he cut each cake?

A common denominator is a common multiple of the denominators of two or more fractions. Fractions with common denominators represent wholes cut into the same number of pieces.


## $(1$ Activity Use paper folding and shading.

Materials $\quad 2$ sheets of paper
Find a common denominator for $\frac{1}{2}$ and $\frac{1}{3}$.

## STEP 1

Model the cake cut into $\frac{1}{2}$-size pieces. Fold one sheet of paper in half. Draw a line on the fold.

## STEP 2

Model the cake cut into $\frac{1}{3}$-size pieces. Fold the other sheet of paper into thirds. Draw lines on the folds.

## STEP 3

Fold each sheet of paper so that both sheets have the same number of parts. Draw lines on the folds. How many equal
$\qquad$ —

## STEP 4

Draw a picture of your sheets of paper to show how many pieces each cake could have.

So, each cake could be cut into $\qquad$ pieces.

## P Example Write $\frac{4}{5}$ and $\frac{1}{2}$ as a pair of fractions with common denominators.

You can use common multiples to find a common denominator.
List multiples of each denominator. A common multiple can be used as a common denominator.

STEP 1 List multiples of 5 and 2.
5: 5 ,
10,
$2:$ $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$

STEP 2 Write equivalent fractions.
$\frac{4}{5}=\frac{4 x}{5 x}=\frac{}{10}$
$\frac{1}{2}=\frac{1 x}{2 x}=\frac{}{10}$
Choose a denominator that is a common multiple of 5 and 2 .

You can write $\frac{4}{5}$ and $\frac{1}{2}$ as $\qquad$ and $\qquad$ .

1. Are $\frac{4}{5}$ and $\frac{1}{2}$ equivalent? Explain.
$\qquad$
$\qquad$

## ERROR Alert

Remember that when you multiply the denominator by a factor, you must multiply the numerator by the same factor to write an equivalent fraction.
2. Describe another way you could tell whether $\frac{4}{5}$ and $\frac{1}{2}$ are equivalent.
$\qquad$
$\qquad$
$\qquad$

## Share and Show

1. Find a common denominator for $\frac{1}{3}$ and $\frac{1}{12}$ by dividing each whole into the same number of equal parts.
Use the models to help.

common denominator: $\qquad$

$\frac{1}{3}$
$\frac{1}{3}$
$\frac{1}{12}$

Name $\qquad$
Write the pair of fractions as a pair of fractions with a common denominator.
2. $\frac{1}{2}$ and $\frac{1}{4}$
3. $\frac{3}{4}$ and $\frac{5}{8}$
4. $\frac{1}{3}$ and $\frac{1}{4}$
5. $\frac{4}{12}$ and $\frac{5}{8}$

## On Your Own

Write the pair of fractions as a pair of fractions with a common denominator.
6. $\frac{1}{4}$ and $\frac{5}{6}$
7. $\frac{3}{5}$ and $\frac{4}{10}$

Tell whether the fractions are equivalent. Write $=$ or $\neq$.
8. $\frac{3}{4} \bigcirc \frac{1}{2}$
9. $\frac{3}{4} \bigcirc \frac{6}{8}$
10. $\frac{1}{2} \bigcirc \frac{4}{8}$
11. $\frac{6}{8} \bigcirc \frac{4}{8}$
12. $\frac{1}{3} \bigcirc \frac{2}{6}$
13. $\frac{1}{3} \bigcirc \frac{4}{12}$
14. $\frac{2}{6} \bigcirc \frac{4}{12}$
15. $\frac{4}{12} \bigcirc \frac{4}{12}$

## Problem Solving REAL WORLD

16. Sense or Nonsense? Carrie has a red streamer that is $\frac{3}{4}$ yard long and a blue streamer that is $\frac{5}{6}$ yard long. She says the streamers are the same length. Does this make sense? Explain.
$\qquad$
$\qquad$
17. H.O.I. Leah has two same-size rectangles divided into the same number of equal parts. One rectangle has $\frac{1}{3}$ of the parts shaded, and the other has $\frac{2}{5}$ of the parts shaded. What is the least number of parts into which both rectangles could be divided?
$\qquad$
18. H.O.T. What's the Error? Jonah says a common denominator for $\frac{3}{4}$ and $\frac{2}{5}$ is 9 . What is Jonah's error? Explain.
$\qquad$
$\qquad$
19. Test Prep Kevin practiced his trumpet $\frac{2}{3}$ hour on Tuesday and $\frac{3}{4}$ hour on Thursday. Which number below is a common denominator for $\frac{2}{3}$ and $\frac{3}{4}$ ?
(A) 2
(C) 8
(B) 4
(D) 12

## Problem Solving • Find Equivalent Fractions

Essential Question How can you use the strategy make a table to solve problems using equivalent fractions?

## 3 UNLOCK the Problem REAL WORLD

Anaya is planting a flower garden. The garden will have no more than 12 equal sections. $\frac{3}{4}$ of the garden will have daisies. What other fractions could represent the part of the garden that will have daisies?

## Read the Problem

## What do I need to find?

$\qquad$ that could
represent the part of the garden that will have daisies

What information do I need to use?
$\qquad$ of the garden will have daisies. The garden will not have more than
equal sections.

## How will I use the information?

I can make a $\qquad$
to find $\qquad$ fractions to solve the problem.

## Solve the Problem



I can make a table and draw models to find equivalent fractions.

1. What other fractions could represent the part of the garden that will have daisies? Explain. $\qquad$
$\qquad$
$\qquad$
$\qquad$

## 1 Try Another Problem

Two friends are knitting scarves. Each scarf has 3 rectangles, and $\frac{2}{3}$ of the rectangles have stripes. If the friends are making 10 scarves, how many rectangles do they need? How many rectangles will have stripes?

## Read the Problem

What do I need to find?

What information do I need to use?

How will I use the information?

## Solve the Problem

2. Does your answer make sense? Explain how you know.

## Share and Show

1. Keisha is helping plan a race route for a 10-kilometer charity run. The committee wants to set up the
$\qquad$ following things along the course.

Viewing areas: At the end of each half of the course
Water stations: At the end of each fifth of the course
Distance markers: At the end of each tenth of the course

Which locations have more than one thing located there?
First, make a table to organize the information.

|  | Number of Locations | First Location | All the Locations |
| :--- | :--- | :--- | :--- |
| Viewing Areas | 2 | $\frac{1}{2}$ | $\frac{1}{2}$ |
| Water Stations | 5 | $\frac{1}{5}$ | $\frac{1}{5}$ |
| Distance Markers | 10 | $\frac{1}{10}$ | $\frac{1}{10}$ |

Next, identify a relationship. Use a common denominator, and find equivalent fractions.

Finally, identify the locations at which more than one thing will be set up. Circle the locations.
$\qquad$
$\qquad$
2. H.O.I. What if distance markers will also be placed at the end of every fourth of the course? Will any of those markers be set up
 at the same location as another distance marker, a water station, or a viewing area? Explain. $\qquad$
3. Fifty-six students signed up to volunteer for the race. There were 4 equal groups of students, and each group had a different task.

How many students were in each group? $\qquad$

## On Your Own

Choose a STRATEGY
4. Andy cut a tuna sandwich and a chicken sandwich into a total of 15 same-size pieces. He cut the tuna sandwich into 9 more pieces than the chicken sandwich. Andy ate 8 pieces of the tuna sandwich. What fraction of the tuna sandwich did he eat?
5. A baker cut a pie in half. He cut each half into 3 equal pieces and each piece into 2 equal slices. He sold 6 slices. What fraction of the pie did the baker sell?
6. H.O.T. Write Math Luke threw balls into these buckets at a carnival. The number on the bucket gives the number of points for each throw. What is the least number of throws needed to score exactly 100 points? Explain.


## SHOW YOUR WORK

7. H.O. A number has exactly eight factors. Two of the factors are 10 and 14 . What is the number, and what are all of the factors?
8. Test Prep A comic-book store will trade 5 of its comic books for 6 of yours. How many of its comic books will the store trade for 36 of yours?
(A) 25
(B) 30
(C) 36
(D) 42
$\qquad$

## Mid-Chapter Checkpoint

## Vocabulary

Choose the best term from the box.

1. $\qquad$ name the same amount. (p. 227)
2. $A$ $\qquad$ is a common multiple of two or more denominators. (p. 239)

## Concepts and Skills

Write two equivalent fractions.
3. $\frac{2}{5}=$ $\qquad$ $=$ $\qquad$
4. $\frac{1}{3}=$ $\qquad$ $=$
5. $\frac{3}{4}=$ $\qquad$ $=$

## Vocabulary

common denominator equivalent fractions factor

Tell whether the fractions are equivalent. Write $=$ or $\neq$.
6. $\frac{2}{3} \bigcirc \frac{4}{12}$
7. $\frac{5}{6} \bigcirc \frac{10}{12}$
8. $\frac{1}{4} \bigcirc \frac{4}{8}$

Write the fraction in simplest form.
9. $\frac{6}{8}$
10. $\frac{25}{100}$
11. $\frac{8}{10}$

Write the pair of fractions as a pair of fractions with a common denominator.
12. $\frac{3}{10}$ and $\frac{2}{5}$
13. $\frac{1}{3}$ and $\frac{3}{4}$

Fill in the bubble completely to show your answer.
14. Sam needs $\frac{5}{6}$ cup mashed bananas and $\frac{3}{4}$ cup mashed strawberries for a recipe. He wants to find whether he needs more bananas or more strawberries. How can he write $\frac{5}{6}$ and $\frac{3}{4}$ as a pair of fractions with a common denominator?
(A) $\frac{5}{12}$ and $\frac{3}{12}$
(B) $\frac{15}{18}$ and $\frac{15}{20}$
(C) $\frac{10}{12}$ and $\frac{9}{12}$
(D) $\frac{10}{12}$ and $\frac{18}{24}$
15. Karen will divide her garden into equal parts. She will plant corn in $\frac{8}{12}$ of the garden. What is the fewest number of parts she can divide her garden into?
(A) 1
(B) 2
(C) 3
(D) 4
16. Olivia is making scarves. Each scarf will have 5 rectangles, and $\frac{2}{5}$ of the rectangles will be purple. How many purple rectangles does she need for 3 scarves?
(A) 5
(B) 6
(C) 7
(D) 10
17. Paul needs to buy $\frac{5}{8}$ pound of peanuts. The scale at the store measures parts of a pound in sixteenths. Which measure is equivalent to $\frac{5}{8}$ pound?
(A) $\frac{5}{16}$ pound
(B) $\frac{8}{16}$ pound
(C) $\frac{10}{16}$ pound
(D) $\frac{15}{16}$ pound
$\qquad$

## Compare Fractions Using Benchmarks

Essential Question How can you use benchmarks to compare fractions?

## UNLOCK the Problem REAL WORLD

Zach made a popcorn snack. He mixed $\frac{5}{8}$ gallon of popcorn with $\frac{1}{2}$ gallon of dried apple rings. Did he use more dried apple rings or more popcorn?

## P. Activity compare $\frac{5}{8}$ and $\frac{1}{2}$.

Materials ■ fraction strips
Use fraction strips to compare $\frac{5}{8}$ and $\frac{1}{2}$. Record on the model below.

| $\overline{2}$ | $\frac{1}{2}$ |  |  |  | $\frac{1}{2}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{5}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ |

$\frac{5}{8} \bigcirc \frac{1}{2}$
So, Zach used more $\qquad$ .

1. Write five fractions equivalent to $\frac{1}{2}$. What is the relationship between the numerator and the denominator of fractions equivalent to $\frac{1}{2}$ ?
 number of eighth-size parts in $\frac{5}{8}$ is related to the number of eighth-size parts you need to make $\frac{1}{2}$.
$\qquad$
$\qquad$
2. How many eighths are equivalent to $\frac{1}{2}$ ?
3. How can you compare $\frac{5}{8}$ and $\frac{1}{2}$ without using a model?
$\qquad$
$\qquad$

Benchmarks A benchmark is a known size or amount that helps you understand a different size or amount. You can use $\frac{1}{2}$ as a benchmark to help you compare fractions.

## $(1$ Example Use benchmarks to compare fractions.

A family hiked the same mountain trail. Evie and her father hiked $\frac{5}{12}$ of the trail before they stopped for lunch. Jill and her mother hiked $\frac{9}{10}$ of the trail before they stopped for lunch. Who hiked farther before lunch?

Compare $\frac{5}{12}$ and $\frac{9}{10}$ to the benchmark $\frac{1}{2}$.


STEP 1 Compare $\frac{5}{12}$ to $\frac{1}{2}$.


Think: Shade $\frac{5}{12}$.


STEP 2 Compare $\frac{9}{10}$ to $\frac{1}{2}$.


Think: Shade $\frac{9}{10}$.


Since $\frac{5}{12}$ is $\qquad$ than $\frac{1}{2}$ and $\frac{9}{10}$ is $\qquad$ than $\frac{1}{2}$, you know that $\frac{5}{12} \bigcirc \frac{9}{10}$. So, $\qquad$ hiked farther before lunch.
4. Explain how you can tell $\frac{5}{12}$ is less than $\frac{1}{2}$ without using a model.
$\qquad$
$\qquad$
5. Explain how you can tell $\frac{7}{10}$ is greater than $\frac{1}{2}$ without using a model.
$\qquad$
$\qquad$
$\qquad$

## Share and Show <br> MATH

1. Compare $\frac{2}{5}$ and $\frac{1}{8}$. Write $<$ or $>$.


|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |


|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$$
\frac{2}{5} \bigcirc \frac{1}{8}
$$

Compare. Write $<$ or $>$.
$\sigma$
2. $\frac{1}{2} \bigcirc \frac{4}{6}$
3. $\frac{3}{10} \bigcirc \frac{1}{2}$
4. $\frac{11}{12} \bigcirc \frac{4}{8}$
5. $\frac{5}{8} \bigcirc \frac{2}{5}$

## Mathematical practices Explain how you <br> On Your Own

Compare. Write $<$ or $>$.
6. $\frac{8}{10} \bigcirc \frac{3}{8}$
7. $\frac{1}{3} \bigcirc \frac{7}{12}$
8. $\frac{2}{6} \bigcirc \frac{7}{8}$
9. $\frac{4}{8} \bigcirc \frac{2}{10}$
10. $\frac{3}{4} \bigcirc \frac{1}{2}$
11. $\frac{6}{6} \bigcirc \frac{1}{3}$
12. $\frac{4}{5} \bigcirc \frac{1}{6}$
13. $\frac{5}{8} \bigcirc \frac{9}{10}$

## H.O.T. Algebra Find a numerator that makes the statement true.

14. $\frac{2}{4}<\frac{}{6}$
15. $\frac{8}{10}>\frac{}{8}$
16. $\frac{10}{12}>\frac{}{4}$
17. $\frac{2}{5}<\frac{}{10}$
18. When two fractions are between 0 and $\frac{1}{2}$, how do you know which fraction is greater? Explain.
$\qquad$
$\qquad$
$\qquad$

## Problem Solving REAL WORLD

19. A group of students ate $\frac{5}{12}$ of a large pepperoni SHOW YOUR WORK
20. Tim ran $\frac{4}{8}$ mile. Lucy ran $\frac{7}{10}$ mile.

Who ran farther?
21. H.O.T. What's the Question? Selena ran farther than Manny.
$\qquad$
$\qquad$
$\qquad$
22. Mary made a small pan of ziti and a small pan of lasagna. She cut the ziti into 8 equal parts and the lasagna into 9 equal parts. Her family ate $\frac{2}{3}$ of the lasagna. If her family ate more lasagna than ziti, what fraction of the ziti could have been eaten?
23. What's the Error? Tom has two pieces of wood to build a birdhouse. One piece is $\frac{3}{4}$ yard long. The other piece is $\frac{4}{8}$ yard long. Tom says both pieces of wood are the same length. Explain his error.
$\qquad$
$\qquad$
24. Test Prep Todd is using the benchmark $\frac{1}{2}$ to compare fractions. Which statement is NOT correct?
(A) $\frac{5}{6}<\frac{1}{2}$
(C) $\frac{5}{6}>\frac{1}{2}$
(B) $\frac{3}{6}=\frac{1}{2}$
(D) $\frac{5}{6} \neq \frac{1}{2}$
$\qquad$

## Compare Fractions

Essential Question How can you compare fractions?

## UNLOCK the Problem

Every year, Avery's school has a fair. This year, $\frac{3}{8}$ of the booths had face painting and $\frac{1}{4}$ of the booths had sand art. Were there more booths with face painting or sand art?

Compare $\frac{3}{8}$ and $\frac{1}{4}$.

## 9 One Way Use a common denominator.



When two fractions have the same denominator, they have equal-size parts. You can compare the number of parts.

## THINK

Think: 8 is a multiple of both 4 and 8 . Use 8 as a common denominator.

$$
\frac{1}{4}=\frac{1 \times}{4 \times}=\frac{}{8}
$$

$\frac{3}{8}$ already has 8 as a denominator.

## MODEL AND RECORD

Shade the model. Then compare.


## ( Another Way Use a common numerator.

When two fractions have the same numerator, they represent the same number of parts. You can compare the size of the parts.

THINK
Think: 3 is a multiple of both 3 and 1 .
Use 3 as a common numerator.
$\frac{3}{8}$ already has 3 as a numerator.

$$
\frac{1}{4}=\frac{1 \times}{4 \times}=\frac{3}{\square}
$$

## MODEL AND RECORD

Shade the model. Then compare.

$\frac{3}{8}$

$\frac{3}{12}$

Since $\frac{3}{8} \bigcirc \frac{1}{4}$, there were more booths with $\qquad$ .

Try This! Compare the fractions. Explain your reasoning.
(A) $\frac{3}{4} \bigcirc \frac{1}{3}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

C $\frac{3}{4} \bigcirc \frac{7}{8}$
$\qquad$

1. Which would you use to compare $\frac{11}{12}$ and $\frac{5}{6}$, a common numerator or a common denominator? Explain.
$\qquad$
$\qquad$
2. Can you use simplest form to compare $\frac{8}{10}$ and $\frac{3}{5}$ ? Explain.
$\qquad$ $\longrightarrow$
$\qquad$

## Share and Show

1. Compare $\frac{2}{5}$ and $\frac{1}{10}$.

Think: Use $\qquad$ as a common denominator.

$$
\begin{aligned}
& \frac{2}{5}=\frac{\times}{\times}= \\
& \frac{1}{10}
\end{aligned}
$$

Think: 4 tenth-size parts $\square$ 1 tenth-size part.
$\frac{2}{5} \bigcirc \frac{1}{10}$
2. Compare $\frac{6}{10}$ and $\frac{3}{4}$.

Think: Use $\qquad$ as a common numerator.
$\frac{6}{10}$
$\frac{3}{4}=\frac{\times}{\times}=\square$
Think: A tenth-size part $\bigcirc$ an eighth-size part. $\frac{6}{10} \bigcirc \frac{3}{4}$

Compare. Write $<,>$, or $=$.
3. $\frac{7}{8} \bigcirc \frac{2}{8}$
5. $\frac{4}{10} \bigcirc \frac{4}{6}$
6. $\frac{6}{12} \bigcirc \frac{2}{4}$

## On Your Own

な4. $\frac{5}{12} \bigcirc \frac{3}{6}$

Compare. Write $<,>$, or $=$.
7. $\frac{1}{3} \bigcirc \frac{1}{4}$
8. $\frac{4}{5} \bigcirc \frac{8}{10}$
9. $\frac{3}{4} \bigcirc \frac{2}{6}$
10. $\frac{1}{2} \bigcirc \frac{5}{8}$
8


#### Abstract

$\qquad$


 |
14
11. $\frac{3}{10} \bigcirc \frac{2}{4}$
12. $\frac{75}{100}$

$\frac{8}{10}$
13. $\frac{4}{6} \bigcirc \frac{2}{3}$ © Houghton Mifflin Harcourt Publishing Comp

## UNLOCK the Problem REAL WORLD

19. Jerry is making a strawberry smoothie. Which statement about the recipe is true?
(A) The amount of strawberries is greater than the amount of milk.
(B) The amount of milk is less than the amount of cottage cheese.
(C) The amount of strawberries is equal to the amount of cottage cheese.
(D) The amount of vanilla is greater than the amount of sugar.

Strawberry Smoothie 3 ice cubes
$\frac{3}{4}$ cup milk
$\frac{2}{6}$ cup cottage cheese
$\frac{8}{12}$ cup strawberries
$\frac{1}{4}$ teaspoon vanilla
$\frac{1}{8}$ teaspoon sugar

a. What do you need to find? $\qquad$
b. How will you find the answer? $\qquad$
c. Show your work.
d. Fill in the bubble for the correct answer choice above.
20. The number of floats in a parade is a prime number. Which of the following could be the number of floats?
(A) 16
(C) 41
(B) 21
(D) 60
21. A kite reached a height of $\frac{4}{12}$ mile. What is $\frac{4}{12}$ in simplest form?
(A) $\frac{1}{4}$
(C) $\frac{1}{3}$
(B) $\frac{2}{6}$
(D) $\frac{1}{2}$
$\qquad$

## Compare and Order Fractions

Essential Question How can you order fractions?

## UNLOCK the Problem REAL wORLD

Jody has equal-size bins for the recycling center. She filled $\frac{3}{5}$ of a bin with plastics, $\frac{1}{12}$ of a bin with paper, and $\frac{9}{10}$ of a bin with glass. Which bin is the

- Underline what you need to find.
- Circle the fractions you will compare. most full?


## Math Idea

Sometimes it is not reasonable to find the exact location of a point on a number line. Benchmarks can help you find approximate locations.

STEP 1 Compare each fraction to $\frac{1}{2}$.
 and $\quad$ are both greater than $\frac{1}{2}$. is less than $\frac{1}{2}$.

Label $\frac{1}{12}$ on the number line above.

STEP 2 Compare $\frac{3}{5}$ and $\frac{9}{10}$.
Think: Use 10 as a common denominator.

$$
\frac{3}{5}=\frac{x}{x}=\square
$$

Since $\frac{6}{10} \bigcirc \frac{9}{10}$, you know that $\frac{3}{5} \bigcirc \frac{9}{10}$.
Label $\frac{3}{5}$ and $\frac{9}{10}$ on the number line above.

The fraction the greatest distance from 0 has the greatest value.
The fraction with the greatest value is $\qquad$ .

So, the bin with $\qquad$ is the most full.

- Compare the distance between $\frac{3}{5}$ and 0 and the distance know you located $\frac{3}{5}$ on the number line correctly. between $\frac{9}{10}$ and 0 . What can you conclude about the relationship between $\frac{3}{5}$ and $\frac{9}{10}$ ? Explain.

P Example 2 Write $\frac{7}{10}, \frac{1}{3}, \frac{7}{12}$, and $\frac{8}{10}$ in order from least to greatest.


STEP 1 Compare each fraction to $\frac{1}{2}$.
List fractions that are less than $\frac{1}{2}$ : $\qquad$
List fractions that are greater than $\frac{1}{2}$ : $\qquad$
The fraction with the least value is $\qquad$ .

Locate and label $\frac{1}{3}$ on the number line above.
STEP 2 Compare $\frac{7}{10}$ to $\frac{7}{12}$ and $\frac{8}{10}$.

Think: $\frac{7}{10}$ and $\frac{7}{12}$ have a common numerator.


Think: $\frac{7}{10}$ and $\frac{8}{10}$ have a common denominator.


Locate and label $\frac{7}{10}, \frac{7}{12}$, and $\frac{8}{10}$ on the number line above.
The fractions in order from least to greatest are $\qquad$ .

So, $\qquad$ $<$ $\qquad$ $<$ $\qquad$ $<$ $\qquad$ _.

Try This! Write $\frac{3}{4}, \frac{3}{6}, \frac{1}{3}$, and $\frac{2}{12}$ in order from least to greatest.

$\qquad$

## Share and Show

## MATH

1. Locate and label points on the number line to help you write $\frac{3}{10}, \frac{11}{12}$, and $\frac{5}{8}$ in order from least to greatest.


Write the fraction with the greatest value.
2. $\frac{7}{10}, \frac{1}{5}, \frac{9}{10}$
3. $\frac{5}{6}, \frac{7}{12}, \frac{7}{10}$
4. $\frac{2}{8}, \frac{1}{8}, \frac{2}{4}, \frac{2}{6}$

Write the fractions in order from least to greatest.
5. $\frac{1}{4}, \frac{5}{8}, \frac{1}{2}$
6. $\frac{3}{5}, \frac{2}{3}, \frac{3}{10}, \frac{4}{5}$
7. $\frac{3}{4}, \frac{7}{12}, \frac{5}{12}$

Write the fractions in order from least to greatest.
8. $\frac{2}{5}, \frac{1}{3}, \frac{5}{6}$
9. $\frac{4}{8}, \frac{5}{12}, \frac{1}{6}$
10. $\frac{7}{100}, \frac{9}{10}, \frac{4}{5}$

## H.O.T. Algebra Write a numerator that makes the statement true.

11. $\frac{1}{2}<\frac{}{10}<\frac{4}{5}$
12. $\frac{1}{4}<\frac{5}{12}<\frac{}{6}$
13. $\overline{8}<\frac{3}{4}<\frac{7}{8}$

## UNLOCK the Problem REAL WORLD

14. Nancy, Lionel, and Mavis ran in a 5-kilometer race. The table shows their finish times. In what order did Nancy, Lionel, and Mavis finish the race?
a. What do you need to find?
$\qquad$
$\qquad$
b. What information do you need to solve the problem?

$\qquad$
c. What information is not necessary?
$\qquad$
d. How will you solve the problem?
$\qquad$
$\qquad$
e. Show the steps to solve the problem.
15. Alma used 3 beads to make a necklace. The lengths of the beads are $\frac{5}{6}$ inch, $\frac{5}{12}$ inch, and $\frac{1}{3}$ inch. What are the lengths in order from shortest to longest?
f. Complete the sentences.

The runner who finished first is $\qquad$ .

The runner who finished second is $\qquad$ .

The runner who finished third is $\qquad$ .
16. Test Prep A recipe for Trail Mix includes $\frac{3}{10}$ cup of sunflower seeds, $\frac{1}{2}$ cup of raisins, and $\frac{3}{8}$ cup of granola. Which list shows the amounts from least to greatest?
(A) $\frac{1}{2}$ cup, $\frac{3}{8}$ cup, $\frac{3}{10}$ cup
(B) $\frac{3}{8}$ cup, $\frac{3}{10}$ cup, $\frac{1}{2}$ cup
(C) $\frac{3}{10}$ cup, $\frac{3}{8}$ cup, $\frac{1}{2}$ cup
(D) $\frac{3}{10}$ cup, $\frac{1}{2}$ cup, $\frac{3}{8}$ cup
$\qquad$

## Chapter Review/Test

## Vocabulary

Choose the best term from the box.

1. A $\qquad$ is a common multiple of two or more denominators. (p. 239)
2. A fraction is in $\qquad$ when the numerator and denominator have only 1 as a common factor. (p. 236)

## Vocabulary

## benchmark

3. A $\qquad$ is a known size or amount that
helps you understand another size or amount. (p. 250)

## Concepts and Skills

Write two equivalent fractions.
4. $\frac{4}{6}=$ $\qquad$ $=$
5. $\frac{6}{10}=$ $\qquad$ $=$
6. $\frac{2}{8}=$ $\qquad$ $=$ $\qquad$

Write each pair of fractions as a pair of fractions with a common denominator.
7. $\frac{3}{4}$ and $\frac{7}{8}$
8. $\frac{2}{3}$ and $\frac{1}{4}$
9. $\frac{7}{10}$ and $\frac{4}{5}$

Compare. Write $<,>$, or $=$.
10. $\frac{5}{8} \bigcirc \frac{5}{12}$
11. $\frac{10}{12} \bigcirc \frac{5}{6}$
12. $\frac{1}{2} \bigcirc \frac{3}{10}$
13. $\frac{1}{4} \bigcirc \frac{1}{3}$

Write the fractions in order from least to greatest.
14. $\frac{2}{3}, \frac{3}{4}, \frac{1}{6}$
15. $\frac{7}{10}, \frac{4}{5}, \frac{1}{2}, \frac{4}{12}$

Fill in the bubble completely to show your answer.
16. Paco needs at least $\frac{3}{8}$ yard of twine to build a model ship. How much twine could he buy?
(A) $\frac{3}{10}$ yard
(B) $\frac{1}{4}$ yard
(C) $\frac{3}{5}$ yard
(D) $\frac{1}{8}$ yard
17. Rachel, Nancy, and Diego were in a fishing competition.

Rachel's fish was $\frac{7}{8}$ foot long, Nancy's fish was $\frac{1}{4}$ foot long, and Diego's fish was $\frac{1}{2}$ foot long. What are the lengths of the fish in order from least to greatest?
(A) $\frac{7}{8}$ foot, $\frac{1}{2}$ foot, $\frac{1}{4}$ foot
(B) $\frac{1}{2}$ foot, $\frac{7}{8}$ foot, $\frac{1}{4}$ foot
(C) $\frac{7}{8}$ foot, $\frac{1}{4}$ foot, $\frac{1}{2}$ foot
(D) $\frac{1}{4}$ foot, $\frac{1}{2}$ foot, $\frac{7}{8}$ foot
18. Amy needs $\frac{6}{8}$ gallon of fruit juice to make punch. She needs an equal amount of sparkling water. How much sparkling water does she need?
(A) $\frac{2}{8}$ gallon
(B) $\frac{1}{2}$ gallon
(C) $\frac{2}{3}$ gallon
(D) $\frac{3}{4}$ gallon
19. Gavin is building a model of a kitchen. In the model, $\frac{2}{5}$ of the floor tiles are white, $\frac{1}{2}$ of the floor tiles are yellow, and $\frac{1}{10}$ of the floor tiles are brown. How many floor tiles could be in the model?
(A) 2
(B) 5
(C) 10
(D) 17

## Fill in the bubble completely to show your answer.

20. Bill has enough money to buy no more than $\frac{1}{2}$ pound of cheese. How much cheese could he buy?
(A) $\frac{1}{3}$ pound
(B) $\frac{4}{6}$ pound
(C) $\frac{5}{8}$ pound
(D) $\frac{3}{4}$ pound
21. Students planted 6 equal-size gardens on Earth Day. They divided each garden into 3 equal sections and planted herbs in 2 of the 3 sections. What fraction of the gardens did the students plant with herbs?
(A) $\frac{3}{6}$
(B) $\frac{2}{6}$
(C) $\frac{6}{18}$
(D) $\frac{12}{18}$
22. Noah and Leslie live the same distance from school. Which could be the distances they live from school?
(A) $\frac{7}{100}$ kilometer and $\frac{7}{10}$ kilometer
(B) $\frac{5}{10}$ kilometer and $\frac{1}{5}$ kilometer
(C) $\frac{80}{100}$ kilometer and $\frac{8}{10}$ kilometer
(D) $\frac{6}{10}$ kilometer and $\frac{2}{5}$ kilometer
23. Keiko needs $\frac{8}{12}$ yard of fabric to finish her quilt. What is $\frac{8}{12}$ written in simplest form?
(A) $\frac{4}{6}$
(B) $\frac{2}{3}$
(C) $\frac{3}{4}$
(D) $\frac{1}{2}$

## Constructed Response

24. Sam needs $\frac{4}{6}$ cup of laundry detergent for his laundry. The cap on top of the laundry detergent holds $\frac{1}{3}$ cup. He has 1 capful of detergent. Does he have enough? Explain.
$\qquad$
$\qquad$

## Performance Task

25. The table shows the distances of some places in town from the school.
(A) Are any of the places shown in the table closer than $\frac{1}{2}$ mile to school? Explain how you know.
$\qquad$
$\qquad$

| Distance from School |  |
| :--- | :---: |
| Place | Distance |
| Library | $\frac{3}{5}$ mile |
| Post Office | $\frac{1}{2}$ mile |
| Park | $\frac{3}{4}$ mile |
| Town Hall | $\frac{8}{10}$ mile |

$\qquad$
$\qquad$
B Are any of the places shown in the table the same distance from school? Explain how you know.
$\qquad$

C Which place is farthest from school? Explain.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

