Add and Subtract Parts of a Whole

Justin has $\frac{3}{8}$ pound of cheddar cheese and $\frac{2}{8}$ pound of brick cheese. How much cheese does he have in all?

- **Step 1** Use fraction strips to model the problem. Use three $\frac{1}{8}$ -strips to represent $\frac{3}{8}$ pound of cheddar cheese.
- **Step 2** Join two more $\frac{1}{8}$ -strips to represent the amount of brick cheese.

Step 4 Use the model to write an equation. $\frac{3}{8} + \frac{2}{8} = \frac{5}{8}$

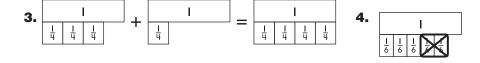
Suppose Justin eats $\frac{1}{8}$ pound of cheese. How much cheese is left?

- **Step 1** Use five $\frac{1}{8}$ -strips to represent the $\frac{5}{8}$ pound of cheese.
- **Step 2** Remove one $\frac{1}{8}$ -strip to show the amount eaten.
- Step 3 Count the number of $\frac{1}{8}$ -strips left. There are $\frac{1}{8}$ fraction strips. There is $\frac{4}{8}$ pound left.

Step 4 Write an equation for the model.

$\frac{5}{8} - \frac{1}{8} = \frac{4}{8}$

Use the model to write an equation.



Write Fractions as Sums

A **unit fraction** tells the part of the whole that 1 piece represents.

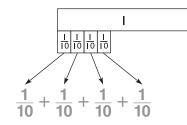
A unit fraction always has a numerator of 1.

Bryan has $\frac{4}{10}$ pound of clay for making clay figures. He wants to use $\frac{1}{10}$ pound of clay for each figure. How many clay figures can he make?

Use fraction strips to write $\frac{4}{10}$ as a sum of unit fractions.

Step 1 Represent $\frac{4}{10}$ with fraction strips.

Step 2 Each $\frac{1}{10}$ is a unit fraction. Write a $\frac{1}{10}$ addend for each $\frac{1}{10}$ -strip you used to show $\frac{4}{10}$.



Step 3 Count the number of addends. The number of addends represents the number of clay figures Bryan can make.

So, Bryan can make ____ clay figures.

Write the fraction as the sum of unit fractions.

1

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2.

$$\frac{3}{6} = + +$$

$$\frac{2}{4}$$
 =



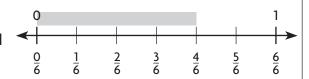
$$\frac{4}{8} = \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}}$$

Add Fractions Using Models

Fractions with like denominators have the same denominator. You can add fractions with like denominators using a number line.

Model $\frac{4}{6} + \frac{1}{6}$.

Step 1 Draw a number line labeled with sixths. Model the fraction $\frac{4}{6}$ by starting at 0 and shading 4 sixths.



Step 2 Add the fraction $\frac{1}{6}$ by shading 1 more sixth.



Step 3 How many sixths are there in all? 5 sixths

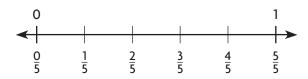
Write the number of sixths as a fraction.

5 sixths =
$$\frac{5}{6}$$
 $\frac{4}{6} + \frac{1}{6} = \frac{5}{6}$

$$\frac{4}{6} + \frac{1}{6} = \frac{5}{6}$$

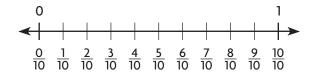
1. Model $\frac{1}{5} + \frac{4}{5}$.



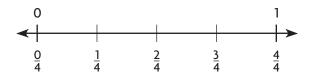


Find the sum. Use a model to help.

2.
$$\frac{2}{10} + \frac{4}{10}$$





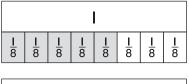


Subtract Fractions Using Models

You can subtract fractions with like denominators using fraction strips.

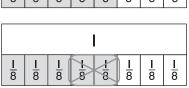
Model
$$\frac{5}{8} - \frac{2}{8}$$
.

Step 1 Shade the eighths you start with. Shade 5 eighths.



Step 2 Subtract $\frac{2}{8}$.

Think: How many eighths are taken away? Cross out **2** of the shaded eighths.



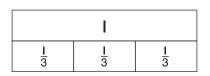
Step 3 Count the shaded eighths that remain. There are 3 eighths remaining.

Step 4 Write the number of eighths that remain as a fraction.

3 eighths
$$=\frac{3}{8}$$
 $\frac{5}{8} - \frac{2}{8} = \frac{3}{8}$

1. Model $\frac{3}{3} - \frac{2}{3}$.





Subtract. Use fraction strips to help.

2.
$$\frac{5}{6} - \frac{1}{6}$$

I									
<u> </u>	<u> </u>	<u>I</u>	<u>I</u>	<u>I</u>	<u>I</u>				

3.
$$\frac{6}{10} - \frac{3}{10}$$



$$\frac{5}{6} - \frac{1}{6} =$$

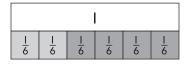
$$\frac{6}{10} - \frac{3}{10} =$$

Add and Subtract Fractions

You can find and record the sums and the differences of fractions.

Add.
$$\frac{2}{6} + \frac{4}{6}$$

Step 1 Model it.



Step 2 Think: How many sixths are there in all?

There are 6 sixths.

6 sixths =
$$\frac{6}{6}$$

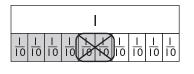
Step 3 Record it.

Write the sum as an addition equation.

$$\frac{2}{6} + \frac{4}{6} = \frac{6}{6}$$

Subtract.
$$\frac{6}{10} - \frac{2}{10}$$

Step 1 Model it.



Step 2 Think: There are 6 tenths. I take away 2 tenths. How many tenths are left?

There are 4 tenths left.

4 tenths =
$$\frac{4}{10}$$

Step 3 Record it.

Write the difference as a subtraction equation.

$$\frac{6}{10} - \frac{2}{10} = \frac{4}{10}$$

Find the sum or difference.

1. 7 eighth-size parts – 4 eighth-size parts = _____

$$\frac{7}{8} - \frac{4}{8} =$$

2.
$$\frac{11}{12} - \frac{4}{12} =$$
 3. $\frac{2}{10} + \frac{2}{10} =$ **4.** $\frac{6}{8} - \frac{4}{8} =$

3.
$$\frac{2}{10} + \frac{2}{10} =$$

4.
$$\frac{6}{8} - \frac{4}{8} =$$

5.
$$\frac{2}{4} + \frac{2}{4} =$$

6.
$$\frac{4}{5} - \frac{3}{5} =$$

5.
$$\frac{2}{4} + \frac{2}{4} =$$
 7. $\frac{1}{3} + \frac{2}{3} =$

Rename Fractions and Mixed Numbers

A **mixed number** is made up of a whole number and a fraction. You can use multiplication and addition to rename a mixed number as a fraction greater than 1.

Rename $2\frac{5}{6}$ as a fraction.

First, multiply the denominator, or the number of parts in the whole, by the whole number.

total number

of parts

$$2 \frac{5}{6} = \frac{17}{6}$$
of parts

number of

parts in the whole

$$6 \times 2 = 12$$

Then, add the numerator to your product.

$$12 + 5 = 17$$

So,
$$2\frac{5}{6} = \frac{17}{6}$$
.

You can use division to write a fraction greater than 1 as a mixed number.

Rename $\frac{16}{3}$ as a mixed number.

To rename $\frac{16}{3}$ as a mixed number, divide the numerator by the denominator.

$$\begin{array}{r}
 5 \\
 \hline
 3) 16 \\
 \hline
 -15 \\
 \hline
 1
 \end{array}$$

Use the quotient and remainder to write a mixed number.

So,
$$\frac{16}{3} = 5\frac{1}{3}$$
.

Write the mixed number as a fraction.

1.
$$3\frac{2}{3} =$$

2.
$$4\frac{3}{5} =$$

1.
$$3\frac{2}{3} =$$
 ____ **2.** $4\frac{3}{5} =$ ____ **3.** $4\frac{3}{8} =$ ____

4.
$$2\frac{1}{6} =$$

Write the fraction as a mixed number.

5.
$$\frac{32}{5} =$$

6.
$$\frac{19}{3} =$$

5.
$$\frac{32}{5} =$$
 6. $\frac{19}{3} =$ **7.** $\frac{15}{4} =$ **8.** $\frac{51}{10} =$ **9.** $\frac{51}{10}$

8.
$$\frac{51}{10} =$$

Add and Subtract **Mixed Numbers**

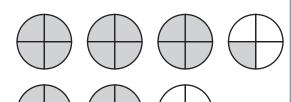
Find the sum. $3\frac{1}{4} + 2\frac{1}{4}$

Add the whole number and fraction parts.

- Add the whole numbers: 3 + 2 = 5• Add the fractions: $\frac{1}{4} + \frac{1}{4} = \frac{2}{4}$

Write the sum as a mixed number, so the fractional

part is less than 1. $3\frac{1}{4} + 2\frac{1}{4} = 5\frac{2}{4}$



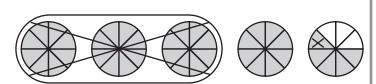
Find the difference. $4\frac{5}{8} - 3\frac{1}{8}$

Subtract the fraction and the whole number parts.

- Subtract the fractions: $\frac{5}{8} \frac{1}{8} = \frac{4}{8}$
- Subtract the whole numbers:

$$4 - 3 = 1$$

$$4\frac{5}{8} - 3\frac{1}{8} = 1\frac{4}{8}$$



Find the sum or difference.

1.
$$3\frac{4}{5}$$

$$+4\frac{3}{5}$$

2.
$$7\frac{2}{3}$$

$$-3\frac{1}{3}$$

3.
$$4\frac{7}{12}$$

$$+6\frac{5}{12}$$

$$-6\frac{1}{4}$$

5.
$$2\frac{3}{8}$$

6.
$$11\frac{9}{10}$$

$$-3\frac{7}{10}$$

7.
$$7\frac{3}{5}$$

$$+4\frac{3}{5}$$

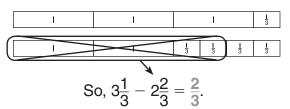
$$-3\frac{1}{6}$$

Subtraction with Renaming

Fraction strips can help you subtract mixed numbers or subtract a mixed number from a whole number.

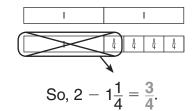
Find the difference. $3\frac{1}{3} - 2\frac{2}{3}$

- **Step 1** Model the number you are subtracting from, $3\frac{1}{3}$.
- **Step 2** Because you cannot subtract $\frac{2}{3}$ from $\frac{1}{3}$ without renaming, change one of the 1 strips to three $\frac{1}{3}$ strips. Then subtract by crossing out two wholes and two $\frac{1}{3}$ strips.



Find the difference. $2 - 1\frac{1}{4}$

- **Step 1** Model the number you are subtracting from, 2.
- **Step 2** Because you cannot subtract $\frac{1}{4}$ from 1 without renaming, change one of the 1 strips to four $\frac{1}{4}$ strips. Then subtract by crossing out one whole and one $\frac{1}{4}$ strip.

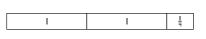


Find the difference.

1.
$$3-2\frac{2}{5}=$$

I	I	I				
I	1	<u>I</u> 5	<u> </u> 5	<u> </u>	<u>I</u> 5	<u>I</u>

2.
$$2\frac{1}{4} - 1\frac{3}{4} =$$



3.
$$3\frac{3}{5}$$
 $-2\frac{4}{5}$

4.
$$3\frac{1}{12}$$
 $-2\frac{11}{12}$

5.
$$4\frac{5}{8}$$
 $-2\frac{7}{8}$

Fractions and Properties of Addition

Properties of addition can help you group and order addends so you can use mental math to find sums.

The Commutative Property of Addition states that when the order of two addends is changed, the sum is the same.

$$6 + 3 = 3 + 6$$

The **Associative Property of Addition** states that when the grouping of addends is changed, the sum is the same.

$$(3+6)+4=3+(6+4)$$

Use the properties and mental math to add $10\frac{3}{8} + 4\frac{7}{8} + 6\frac{5}{8}$.

Step 1 Look for fractions that combine to make 1.

$$10\frac{3}{8} + 4\frac{7}{8} + 6\frac{5}{8}$$

Step 2 Use the Commutative Property to order the addends so that the fractions with a sum of 1 are together.

$$10\frac{3}{8} + 4\frac{7}{8} + 6\frac{5}{8} = 10\frac{3}{8} + 6\frac{5}{8} + 4\frac{7}{8}$$

Step 3 Use the Associative Property to group the addends that you can add mentally.

$$= \left(10\frac{3}{8} + 6\frac{5}{8}\right) + 4\frac{7}{8}$$

Step 4 Add the grouped numbers and then add the other mixed number.

$$= (17) + 4\frac{7}{8}$$

Step 5 Write the sum.

$$=21\frac{7}{8}$$

Use the properties and mental math to find the sum.

1.
$$\left(3\frac{1}{5}+1\frac{2}{5}\right)+4\frac{4}{5}$$

1.
$$\left(3\frac{1}{5}+1\frac{2}{5}\right)+4\frac{4}{5}$$
 2. $\left(5\frac{7}{10}+1\frac{4}{10}\right)+6\frac{3}{10}$ **3.** $7\frac{3}{4}+\left(5+3\frac{1}{4}\right)$

3.
$$7\frac{3}{4} + \left(5 + 3\frac{1}{4}\right)$$

4.
$$\left(2\frac{5}{12}+3\frac{11}{12}\right)+1\frac{7}{12}$$
 5. $4\frac{7}{8}+\left(6\frac{3}{8}+\frac{1}{8}\right)$ **6.** $9\frac{2}{6}+\left(4\frac{1}{6}+7\frac{4}{6}\right)$

5.
$$4\frac{7}{8} + \left(6\frac{3}{8} + \frac{1}{8}\right)$$

6.
$$9\frac{2}{6} + \left(4\frac{1}{6} + 7\frac{4}{6}\right)$$

Problem Solving • Multistep Fraction Problems

Jeff runs $\frac{3}{5}$ mile each day. He wants to know how many days he has to run before he has run a whole number of miles.

Read the Problem Solve the Problem What do I need to find? Describe how to act it out. Use a number line. I need to find how many days Jeff needs to run $\frac{3}{5}$ mile until he has run a whole number of miles. Day 1: $\frac{3}{5}$ mile Day 2: $\frac{6}{5}$ mile $\frac{3}{5}$ + $\frac{3}{5}$ = $\frac{6}{5}$ What information do I need to use? Jeff runs $\frac{\overline{5}}{}$ mile a day. He 1 whole mile and $\frac{1}{5}$ mile more Day 3: $\frac{9}{5}$ mile $\frac{3}{5}$ + $\frac{3}{5}$ + $\frac{3}{5}$ = $\frac{9}{5}$ wants the distance run to be a whole number 1 whole mile and $\frac{4}{5}$ mile more Day 4: $\frac{12}{5}$ mile $\frac{\frac{3}{5}}{5}$ + $\frac{\frac{3}{5}}{5}$ + $\frac{\frac{3}{5}}{5}$ = $\frac{12}{5}$ How will I use the information? 2 whole miles and $\frac{2}{5}$ mile more I can use a number line and patterns to act out Day 5: $\frac{15}{5}$ mile $\frac{3}{5} + \frac{3}{5} + \frac{3}{5} + \frac{3}{5} + \frac{3}{5} = \frac{15}{5}$ the problem. 3 whole miles

- **1.** Lena runs $\frac{2}{3}$ mile each day. She wants to know how many days she has to run before she has run a whole number of miles.
- **2.** Mack is repackaging $\frac{6}{8}$ -pound bags of birdseed into 1-pound bags of birdseed. What is the least number of $\frac{6}{8}$ -pound bags of birdseed he needs in order to fill 1-pound bags without leftovers?

So, Jeff will run a total of 3 miles in 5

davs.